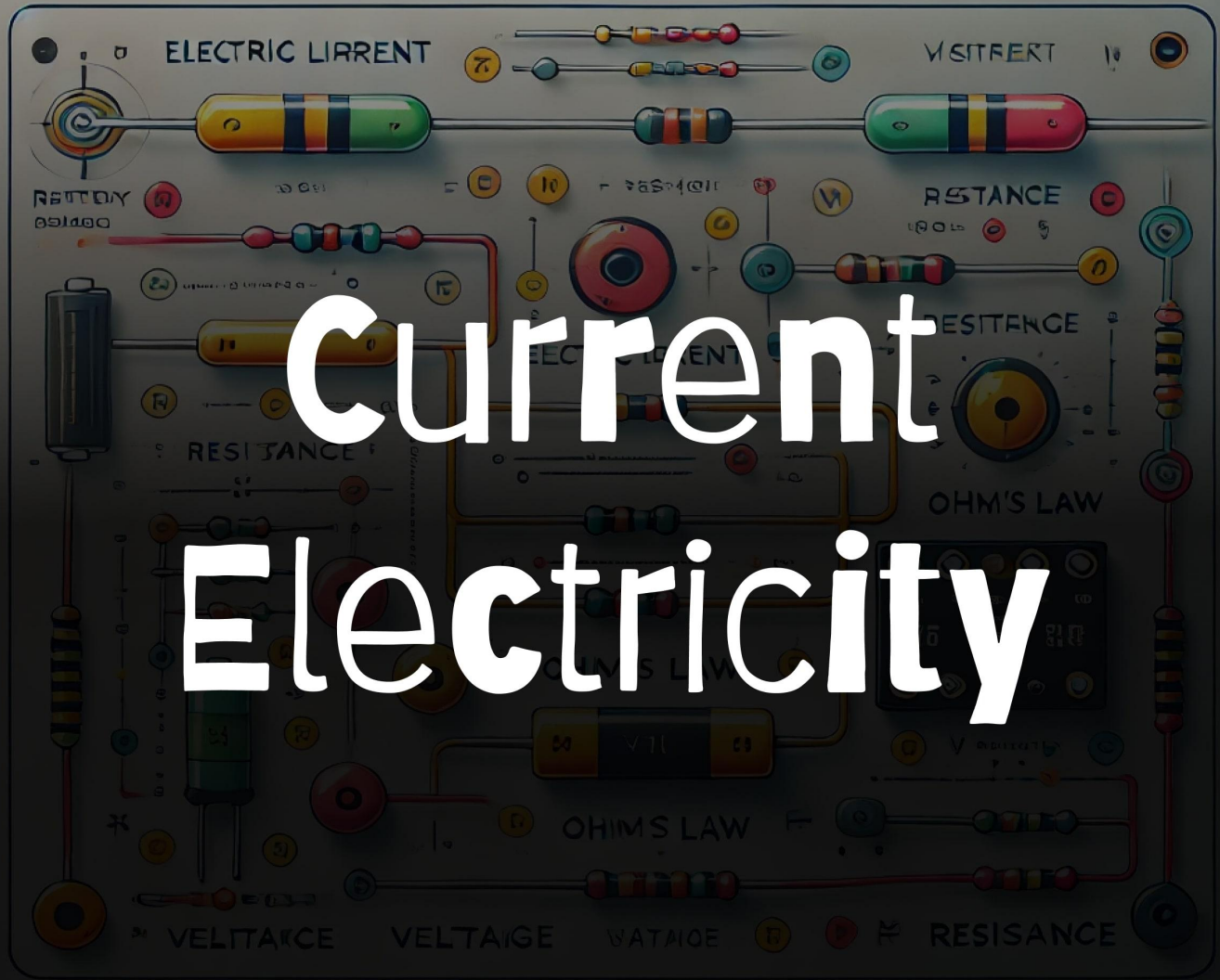




— I/A — 'CURRENT ELECTRICITY — — IR —



Current Electricity

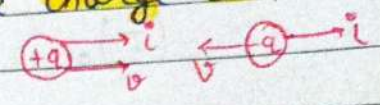
I/A — — V — — IR —

→ - V I - ⚡ || ⚡ - IR -

CURRENT ELECTRICITY

Electric Current \rightarrow The rate of directional flow of electric charge is called electric current.

- \Rightarrow Scalar
- \Rightarrow Direction of current along the motion of +ve charge and opposite to motion of -ve charge
- \Rightarrow Unit (Amp)
- \Rightarrow Dimo (A^2)



Electric Current

$$\int_{t_1}^{t_2} I \cdot dt = \int dq$$

conseq. $Q = I \cdot dt$

$$I_{inst} = \left(\frac{dq}{dt} \right)$$

$$I_{avg} = \frac{\Delta Q}{\Delta t} = \frac{Q_f - Q_i}{t_f - t_i}$$

$$I_{avg} = \frac{\int I dt}{\int dt}$$

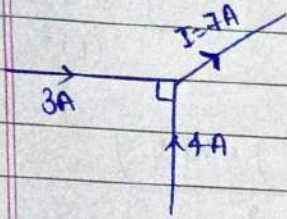
= Slope of q/t graph is current

C.G.S Unit of Current \rightarrow biot

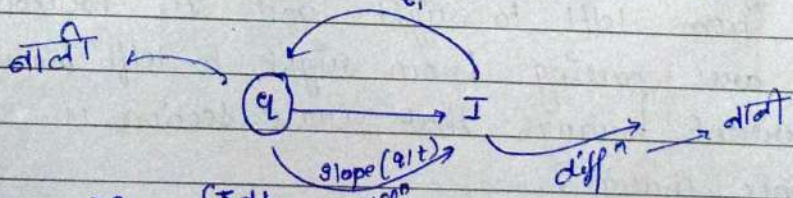
$$1 \text{ Amp} = 10^9 \text{ biot}$$

$$\frac{dq}{dt} = \frac{C}{\text{sec}} \text{ Ampere}$$

Ex!



$$\Delta Q = \int_{t_1}^{t_2} I dt = \text{Area of } (I/t)$$



$$I_{avg} = \frac{\Delta Q}{\Delta t} = \frac{\int I dt}{\int dt}$$

$$I = \frac{dq}{dt}$$

$$\int I dt = \int dq$$

$$\int I dt = \Delta Q$$

Time Period $i = \frac{Q}{T} = Qf$

$$f = \frac{1}{T}$$

$i = Qf$ frequency

Ques If Charge $Q = t^2 + 2t - 4$ is flowing through wire then find current at $t = 2$ sec and 2 sec

$$I = \left(\frac{dQ}{dt} \right) = 2t + 2$$

$$(I)_{at\ t=2} = 2 \times 2 + 2 = 6 \text{ Amp}$$

$$I_{avg} = \frac{\int I dt}{\int dt} = \frac{\Delta Q}{\Delta t}$$

$$\frac{Q_f - Q_i}{t_f - t_i} = \frac{4 - (-4)}{2 - 0} = \frac{8}{2} = 4 \text{ Amp}$$

Ques

If Current flowing through wire $I = 3t^2 + 2t$ then find current at $t = 2$ sec and avg. current in 2 sec

$$I = 3t^2 + 2t$$

$$(I)_{t=2 \text{ sec}} = 3(2)^2 + 2(2) = 3 \times 4 + 4 = 16 \text{ amp}$$

$$I_{avg} = \frac{\int_0^2 I dt}{\int_0^2 dt} = \frac{\int_0^2 (3t^2 + 2t) dt}{(t)_0^2}$$

$$= \frac{3 \left(\frac{t^3}{3} \right) + 2 \left(\frac{t^2}{2} \right)}{2}$$

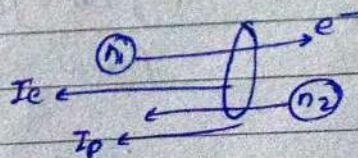
$$\frac{(t^3 + t^2)_0^2}{2} = \frac{8 + 4}{2} = \frac{12}{2} = 6 \text{ amp}$$

Ques Through a given cross section n_1 electrons per second are passing from left to right and n_2 protons per second are passing from right to left simultaneously. The electric current through that cross section is ($e = \text{electronic charge}$).

- (a) $(n_1 + n_2) e$ towards left (b) $(n_2 - n_1) e$ towards right
 (c) $(n_1^2 + n_2^2) e$ towards left (d) $(n_2^2 - n_1^2) e$ towards right

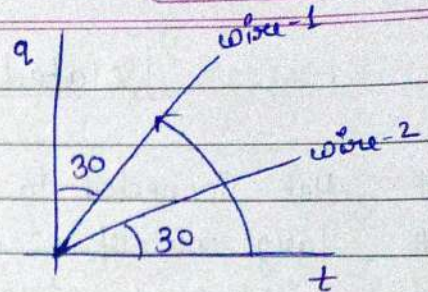
$$I = \frac{\Delta Q}{\Delta t} = \frac{n_1 e}{1 \text{ sec}} + \frac{n_2 e}{1}$$

$$(n_1 + n_2) e$$



Ques ✓ find ratio of current $\frac{I_1}{I_2} = ?$

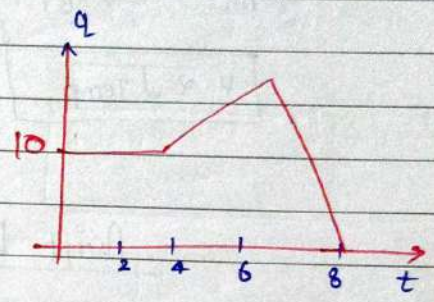
$I = \text{Slope } (q/t) \text{ graph } = \tan \theta$
 $\frac{I_1}{I_2} = \frac{\tan 60^\circ}{\tan 30^\circ}$



$\frac{I_1}{I_2} = \frac{\sqrt{3}}{1/\sqrt{3}} = \boxed{\frac{3}{1}}$ Ans

Ques ✓ find Avg Current b/w 0 to 8 sec.

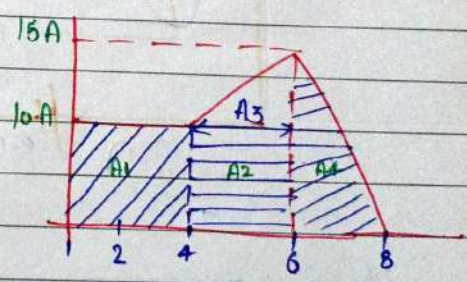
$I_{\text{avg}} = \frac{\Delta q}{\Delta t} = \frac{\int I dt}{\int dt}$
 $(I_{\text{avg}})_{0.8 \text{ sec}} = \frac{q_{t=8} - q_{t=0}}{8 - 0}$



$\frac{0 - 10}{8} = \frac{-10}{8}$ Amp.

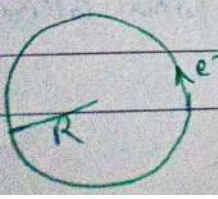
Ques ✓ find avg current b/w 0 to 8 sec

$I_{\text{avg}} = \frac{\int I dt}{\int dt} = \left[\frac{\text{Area } q}{\Delta t} \right]$
 $= \frac{40 + 20 + 5 + 15}{8}$
 $\frac{80}{8} = \underline{10 \text{ Amp}}$



$A_1 = 40$
 $A_2 = 20$
 $A_3 = \frac{1}{2} \times 2 \times 5$
 $A_3 = \frac{1}{2} \times 2 \times 5$

Ques ✓ If electron is moving on the circular path with frequency f then find current.



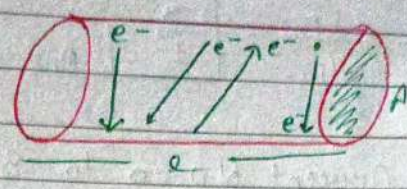
$I = \frac{\Delta q}{\Delta t} = \frac{e}{T} = ef \text{ Amp.}$
 ↗ Clockwise current

$I = \frac{e}{T} = \frac{e}{2\pi R} = \frac{ev}{2\pi R}$

Isolated Conductor

- # Not Connected to the battery. ($\epsilon_{in} = 0$)
- # large no of e^- are in random motion
- # with speed = 10^4 m/sec.

due to thermal energy (Temp).



Path of e^- are straight line

Thermal Speed

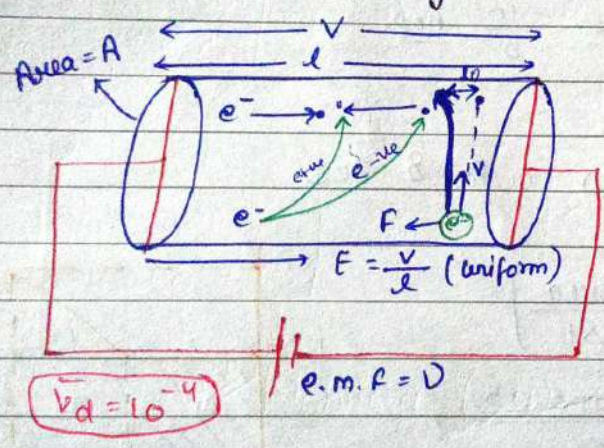
$$\frac{1}{2} m v^2 = \frac{3}{2} k_B T$$

$$v \propto \sqrt{\text{Temp}}$$

$$\langle \text{Velocity} \rangle = 0$$

$$v = \sqrt{\frac{3RT}{m}}$$

Drift Velocity / OHM Law



$$E = \frac{V}{l} \text{ (uniform)}$$

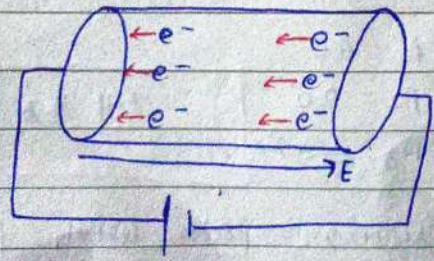
$$\text{force on } e^- = qE = eE$$

$$a = \frac{F}{m} = \frac{eE}{m} \text{ (uniform)}$$

Path of $e^- \rightarrow$ Parabolic

drifted length = l_0
= mean free path.
(avg distⁿ b/w two collision)

EC



Drift Velocities

$$\langle v \rangle = \langle v \rangle_0 + \langle at \rangle$$

$$\langle v \rangle = \frac{eE}{m} \tau$$

Relaxation time

(avg time b/w two collision)

$$v_d = a\tau$$

$$v_d = \frac{eE}{m} \tau$$

or

$$\frac{e \times v \times \tau}{m}$$

Drift Velocity

$$F = eE$$

$$a = \frac{eE}{m}$$

$$V_{\text{drift}} = \frac{eE\tau}{m}$$

$$I = neAV_d$$

elastic
curren

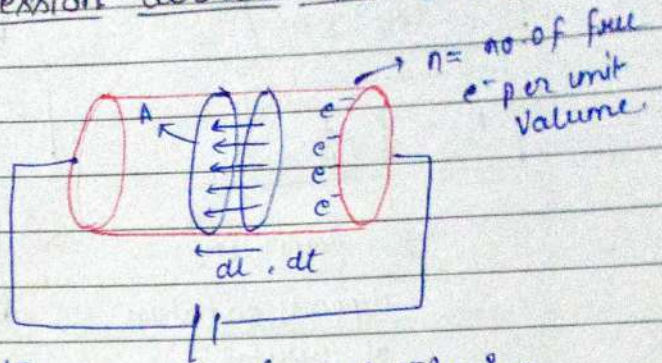
no. of e^- per
unit volume.

$$l = \text{free path}$$

$$V = El = E\lambda$$

$$\text{Energy} = qEl$$

Expression current in term of drift velocity



$$I = \frac{dq}{dt}$$

$$I = nA \left(\frac{dl}{dt} \right) e$$

$$I = neAV_d$$

$N =$ (no. of e^- passing through this cross-section)

$$= nAdl$$

Volume.

$$dq = Ne$$

$$dq = nAde l$$

$$I = neAV_d$$

$$V_d = \frac{I}{neA}$$

$$V_d = \frac{eE\tau}{m}$$

$$I = neAV_d$$

$$V_d = \frac{I}{neA} \quad \text{--- (i)}$$

$$V_d = \frac{eE\tau}{m} \quad \text{--- (ii)}$$

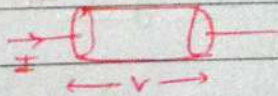
$$\text{(ii)} \text{ --- (i)}$$

$$\frac{eE\tau}{m} = \frac{I}{neA}$$

$$\frac{V}{l} = \frac{mI}{ne^2 A \tau}$$

$$V = \frac{mI}{ne^2 A \tau}$$

microscopic form of Ohm's Law:



$$\text{(iii)} = \text{(iv)}$$

$$\frac{mI}{ne^2 A \tau} = I R$$

$$R = \frac{m l}{ne^2 \tau A}$$

Resistance

$$V \propto I$$

$$V = RI \quad \text{--- (iv)}$$

Ohm's Law

Macroscopic form of Ohm's Law

$$R = \frac{m l}{n e^2 \epsilon A}$$

$$\rho = \frac{m}{n e^2 \epsilon}$$

$$R = \rho \frac{l}{A}$$

$$\sigma \text{ (conductivity)} = \frac{1}{\rho}$$

ρ = Resistivity
depends on nature
of crystal.

$$\sigma = \frac{n e^2 \tau}{m e}$$

Conductivity

$$\sigma = \frac{n e^2 \tau}{m} \text{ --- (i)}$$

$$V = IR \text{ --- (vi)}$$

$$\rho = \frac{1}{\sigma} \text{ --- (ii)}$$

$$V = \frac{m l I}{n e^2 \tau A} \text{ --- (vii)}$$

Resistivity
material

$$\rho = \frac{m}{n e^2 \epsilon} \text{ --- (iii)}$$

$$I = n e A v_d \text{ --- (viii)}$$

$$R = \frac{\rho l}{A} \text{ --- (iv)}$$

$$v_d = \frac{e E \tau}{m} \text{ --- (ix)}$$

$$R = \frac{m l}{n e^2 \tau A} \text{ --- (v)}$$

$$E = \frac{V}{l} \text{ --- (x)}$$

Mobility (μ)

Property of charge particle

$$\mu = \frac{u}{E}$$

Drift Velocity
per unit electric
field.

$$\mu = \frac{e \tau}{m}$$

$$\mu = \frac{e \tau}{m} \text{ mobility}$$

Mobility does not depend
on drift velocity and
electric field.

$$\mu = \frac{e}{m} \propto \text{specific charge}$$

* Proton (e, mp)

$$u_p = \frac{eE}{m}$$

* α -Particle (2p, 2v)
(2e, 4m)

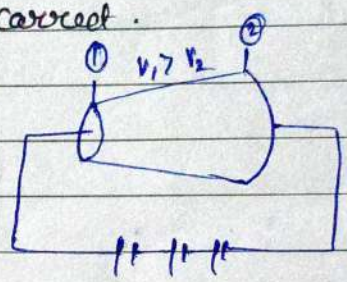
$$u_{\alpha} = \frac{2eE}{4m} = \frac{eE}{2m} = \frac{1}{2} u_p$$

* Deuteron (e, 2m)

$$u_d = \frac{eE}{2m} = \frac{u_p}{2}$$

Q4 The Value of drift speed at Cross section (1) and (2) are v_1 and v_2 respectively in the conductor shown below in the shape of a truncated cone. Which of the following is correct.

$$v_d = \frac{I}{neA}$$



(j) Current Density = electric current per unit area.

$$\vec{J} = \frac{I}{A} = \frac{neAv_d}{A}$$

dirⁿ along the dirⁿ of current
 Vector
 Unit Amp / m²

$$J = ne v_d$$

Putting the value of v_d

$$v_d = \frac{eE\tau}{m} \quad \text{--- (ii)}$$

$$J = ne \left(\frac{eE\tau}{m} \right)$$

$$J = \frac{ne^2\tau}{m} E$$

$$\vec{J} = \sigma \vec{E}$$

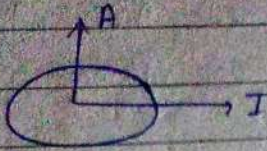
Vector form of Ohm's law

Conductivity $\vec{E} = \vec{E} J$

dirⁿ of \vec{J} along Electric field.

$$J \propto \frac{1}{A}$$

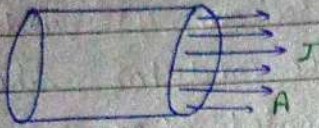
Current density



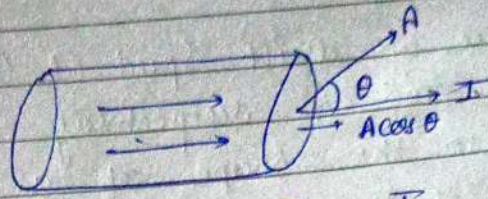
$J = \text{Not define.}$

$$J = \frac{J \cdot A}{A}$$

$$J = \frac{I}{A}$$



$$J = \frac{I}{A}$$



$$J = \frac{I}{A \cos \theta}$$

$$I = J A \cos \theta$$

Current $\rightarrow I = \vec{J} \cdot \vec{A} = \boxed{J A \cos \theta}$

Ques Current density \vec{j} at an area $\vec{A} = (2\hat{i} + 3\hat{j}) \text{ mm}^2$ is $\vec{j} = (3\hat{i} + 4\hat{j}) \text{ A/m}^2$, Current through the area is

① $9 \mu\text{A}$

② Zero

③ $18 \mu\text{A}$ ✓

④ $12 \mu\text{A}$

$$I = \vec{A} \cdot \vec{j}$$

$$(2\hat{i} + 3\hat{j}) \cdot (3\hat{i} + 4\hat{j})$$

$$(6 + 12)$$

$$18 \times 10^{-6}$$

$$= 18 \mu\text{A} \quad \text{B}$$

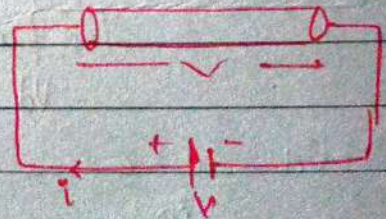
Resistance

$$R \propto I \quad \text{--- (i)}$$

Copper

$$R \propto \frac{I}{A} \quad \text{--- (ii)}$$

Steel



$$R = \frac{\rho A}{A}$$

$\rho = \text{resistivity / specific resistance}$

formula

$$j = \frac{m}{n e^2 \tau}$$

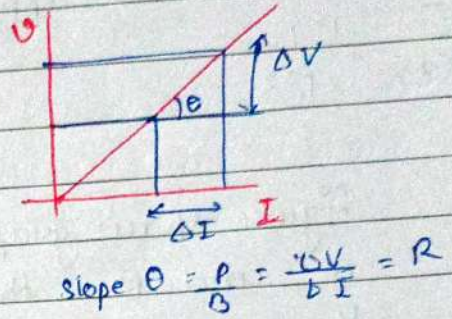
depends on nature of conductor
 does not depend on length and Area.

If length is changes keeping Area = Const

$$R \propto l$$

$$\frac{R_1}{R_2} = \frac{l_1}{l_2}$$

$$\frac{\Delta R}{R} = \frac{\Delta l}{l}$$



If length is changing keeping

I or V constant = Slope $\propto \frac{1}{\text{Resistance}}$

$$\text{Volume} = \text{Const}$$

$$R = \frac{\rho l \times l}{A \times l}$$

$$R = \frac{\rho l^2}{\text{Volume}}$$

$$\Rightarrow R \propto l^2 \Rightarrow \frac{R_1}{R_2} = \frac{l_1^2}{l_2^2}$$

$$\frac{\Delta R}{R} = \frac{2 \Delta l}{l}$$

Area is changing keeping length Const

Area is changing keeping Volume Const

$$R = \frac{\rho l}{A} \text{ const}$$

$$R \propto \frac{1}{A} \propto \frac{1}{r^2} \quad (r = \text{radius})$$

$$\frac{\Delta R}{R} = -\frac{\Delta A}{A} = -2 \frac{\Delta r}{r}$$

$$\frac{R_1}{R_2} = \frac{A_2}{A_1} = \frac{r_2^2}{r_1^2}$$

$$R' = \left(\frac{r'}{r}\right)^2$$

$$R = \frac{\rho l \times A}{A \times A} = \frac{\rho \text{ Volume}}{A^2}$$

$$R \propto \frac{1}{A^2} \propto \frac{1}{r^4}$$

$$\frac{R_1}{R_2} = \frac{A_2^2}{A_1^2} = \frac{r_2^4}{r_1^4}$$

$$\frac{\Delta R}{R} = -\frac{2 \Delta A}{A} = -4 \frac{\Delta r}{r}$$

Two copper wires of length l and $2l$ have radii R and $2R$ respectively. What is the ratio of their specific resistance?

- (a) 1:2
 (b) 2:1
 (c) 1:1 ✓
 (d) 1:3

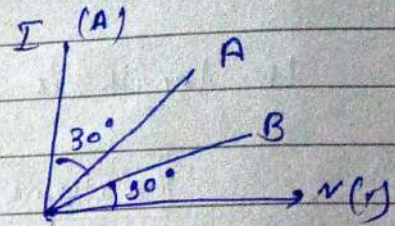
Copper is always same here

The figure shows graph b/w I and V for two conductors A and B. Their respective resistances are in the ratio.

- (1) 1:1
 (2) 1:3 ✓
 (3) 3:1
 (4) 1:2

$$V = IR$$

$$R = \frac{V}{I} \quad (\text{slope of } V/I \text{ graph is ratio})$$



$$\left(\frac{R_A}{R_B}\right) = \frac{\text{Slope B}}{\text{Slope A}} = \frac{\tan 30^\circ}{\tan 60^\circ} = \frac{1}{3}$$

Two wires A and B of the same material having radii in the ratio 1:2 carry current in the ratio 4:1. The ratio of drift speed of electrons in A and B is.

- (a) 16:1 ✓
 (b) 1:16
 (c) 1:4
 (d) 4:1

$$I = neAv_d$$

$$v_d = \frac{I}{A} = \frac{I}{\pi r^2}$$

$$v_d \propto \frac{I}{r^2}$$

$$\frac{v_1}{v_2} = \frac{I_1}{I_2} \left(\frac{r_2^2}{r_1^2}\right) = \frac{4}{1} \left(\frac{2}{1}\right)^2 = 4 \times 4 = 16/1$$

4 If a Copper wire is stretched to make its radius decrease by 0.1%. Then the percentage increase in resistance is nearly.

a) 0.1% $R \propto \frac{1}{R^2} \propto \frac{1}{r^4}$

b) 0.8%

c) 0.4% ✓ $100 \times \frac{\Delta R}{R} = -4 \left(\frac{\Delta r}{r} \right) \times 100$

d) 0.2% $= -4 (-0.1) \%$

$\frac{\Delta R}{R} \times 100 = 0.4\%$

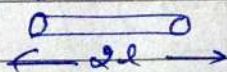
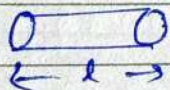
4 A wire of resistance x Ohm is drawn out, so that its length is increased to twice its original length, and its new resistance becomes 20Ω then x will be

a) 5Ω ✓

$R = x \Omega$

$V = \text{const}$ $R' = 20 \Omega$

b) 10Ω



c) 15Ω

d) 20Ω

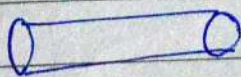
$R \propto l^2$ $\frac{x}{20} = \left(\frac{l}{2l} \right)^2$

$\frac{x}{20} = \frac{1}{4} \Rightarrow x \frac{20}{4} = 5 \Omega$

4 A certain piece of Copper is to be shaped into a conductor of minimum resistance. Its length and diameter should respectively be

a) l, d

b) $2l, \frac{d}{2}$



c) $\frac{l}{2}, 2d$

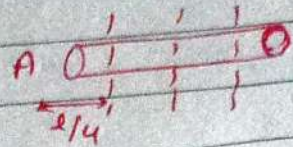
$R_{\min} \propto \frac{l_{\min}}{A_{\max}}$

d) $l, \frac{d}{2}$

A piece of wire is cut into four equal parts and the pieces are bundled together side by side to form a thicker wire. Compared with that of the original wire the resistance of the bundle is

- (a) The same
- (b) 1/16 of much
- (c) 1/8 of much
- (d) 1/4 of much

$$R = \frac{\rho l}{A}$$

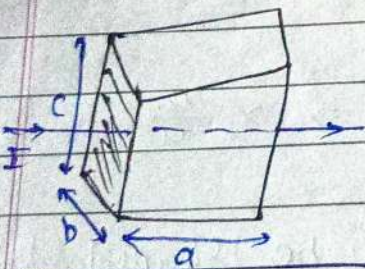
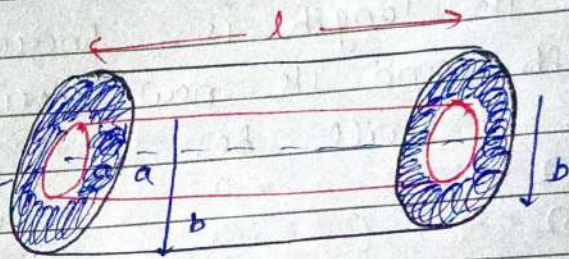


$$R' = \frac{\rho l}{4 \times 4 A} = \frac{R}{16}$$

$$R \propto l$$

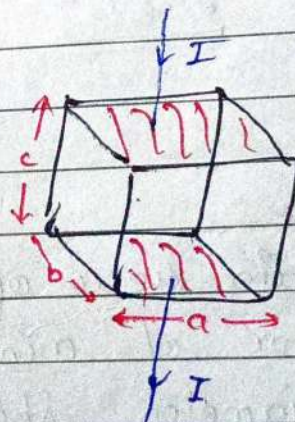
$$R = \frac{\rho l}{A} = \frac{\rho l}{\pi b^2 - \pi a^2}$$

$$R = \frac{\rho l}{\pi (b^2 - a^2)}$$



$$R = \frac{\rho l}{A} = \frac{\rho a}{cb}$$

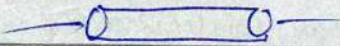
or



$$R = \frac{\rho c}{ab}$$

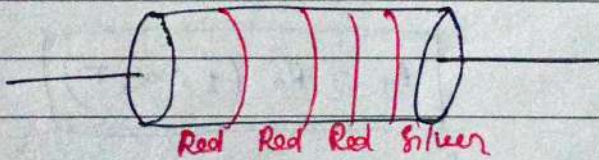
Resistor Colour Codes

0	1	2	3	4	5	6	7	8	9
B.	B.	R.	O.	Y.	G.	B.	V.	G.	Wife
↓	↓	↓	↓	↓	↓	↓	↓	↓	↓
Black	Brown	Red	Orange	Yellow	Green	Blue	Violet	Grey	White
●	●	●	●	●	●	●			



$$R = [52 \times 10^4 \Omega] \pm 10\%$$

Q. Find the resistance of following Carbon resistor



R R R D Y

$$R = [22 \times 10^3 \Omega] \pm 10\%$$

Conductor

Insulator

Semiconductor

Temp ↑

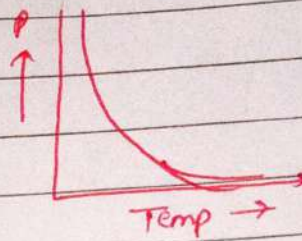
Randomness ↑
Resistivity / Resist ↑
Conductivity ↓
V_{drift} V_{el} ↓

Same as
Semiconductor

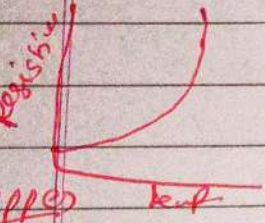
e-hole pair ↑
Resistivity ↓
Conductivity ↑
drift velocity ↓

Temp ↓

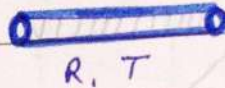
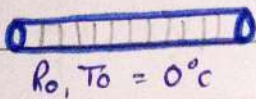
Randomness ↓
Resistivity ↓
Conductivity ↑
drift velocity ↑
= Copper



e-hole pair ↓
Resistivity ↑
Conductivity ↓
drift velocity ↑
Silicon
Graphite



Temperature dependence of Resistance and Resistivity



$$\alpha_R = \frac{\Delta R}{R \Delta T}$$

= Relative change in Resistance per unit raise in temp.

Tempⁿ Coefficient of Resistance

for Conductor $\alpha_R \rightarrow +ve$

for Semiconductor $\alpha_R \rightarrow -ve$

Insulator $-ve$

$$\Delta R \propto R_0 \text{ --- (1)}$$

$$\Delta R \propto \Delta T \propto (T - T_0)$$

$$\Delta R \propto \alpha_R$$

↑
Tempⁿ Coefficient of substance.

$$\Delta R = \alpha_R R_0 \Delta T$$

Change in Resistance

$$\Delta R = R_T - R_0 = R_0 \alpha_R \Delta T$$

$$R_T = R_0 (1 + \alpha_R \Delta T)$$

Resistance at T

Thermal Coefficient of Resistance

Imp

$$\alpha_R = \frac{\Delta R}{R \Delta T}$$

$$R_T = R_0 (1 + \alpha_R T) \quad \text{--- (1)}$$

↳ Resistance at temp T

R_0 = Initial Resistance

α = Temp Coefficient of Resist

Temp Resistivity

$$\alpha_p = \frac{\Delta \rho}{\rho \Delta T}$$

= Relative change in resistivity per unit change temp.

If Resistance at temp T_1 is R_1 and at temp T_2 is R_2 then find relation b/w them where $\alpha_R \rightarrow$ Temp Coefficient of Resistance.

$$R_2 = R_1 [1 + \alpha (T_2 - T_1)] \quad \times$$

Let assume R_0 is temp at 0°C

$$\frac{R_1 = R_0 (1 + \alpha T_1)}{R_2 = R_0 (1 + \alpha T_2)} = \frac{R_1}{R_2} = \left(\frac{1 + \alpha T_1}{1 + \alpha T_2} \right)$$

Q Find Relation b/w $\alpha \rightarrow$ Coefficient of Linear Expansion
 $\alpha_R \rightarrow$ Coefficient of Resistance and $\alpha_p \rightarrow$ Coefficient of Resistivity.

$$R = \frac{\rho l}{A}$$

$$\alpha = \frac{\Delta l}{l \Delta T}$$

change over analysis

$$\alpha_R = \frac{\Delta R}{R \Delta T}$$

$$\frac{\Delta R}{R \Delta T} = \frac{\Delta \rho}{\rho \Delta T} + \frac{\Delta l}{l \Delta T} - \frac{\Delta A}{A \Delta T}$$

$$\alpha_p = \frac{\Delta \rho}{\rho \Delta T}$$

$$\alpha_R = \alpha_p + \alpha - \beta$$

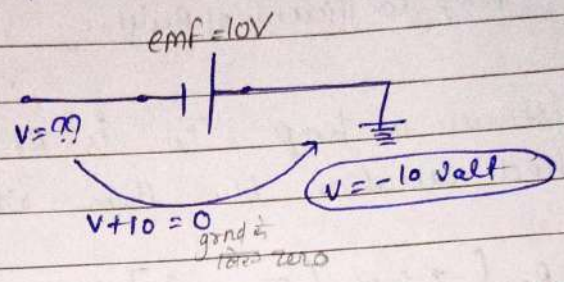
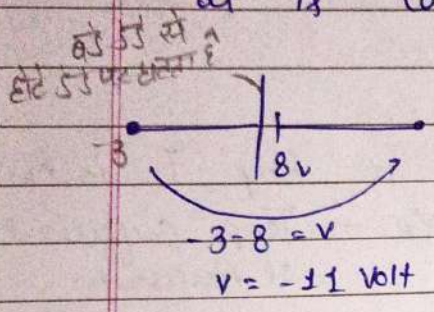
$$\alpha_R = \alpha_p + \alpha - 2\alpha$$

$$\boxed{\alpha_R = \alpha_p - \alpha}$$

Battery → Battery is not a source of charge
→ It is a source of energy.

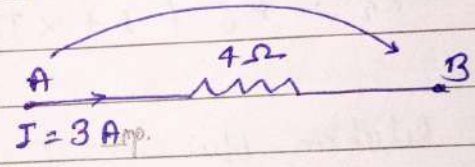
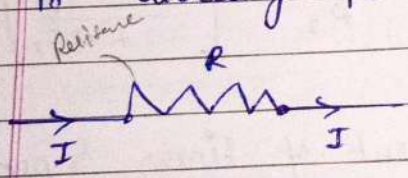
$\omega = 9V$

- Maintain const Potential diffⁿ across point where it is connected.



Potential drop across resistance → Ohm's Law

Potential drop across two end of resistance is directly proportional to current.

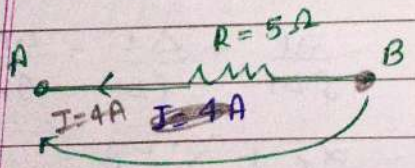


$V = RI$

$V_A > V_B$

$V_A - IR = V_B$
 $V_A - V_B = 3 \times 4 = 12 \text{ Volt}$

Current flow from Higher to lower.



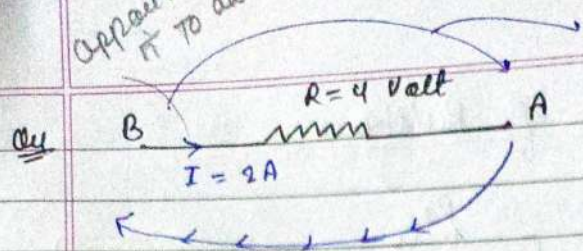
$V_B - 4 \times 5 = V_A$

$-20 \text{ Volt} = V_A - V_B$

$V_B > V_A$

And $V_A - V_B = ??$

Opposite direction \rightarrow to add negative.



$$V_B - IR = V_A$$

$$- 2 \times 4 = V_A - V_B$$

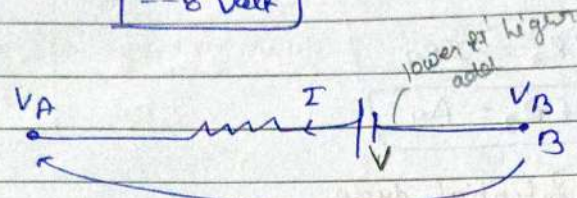
$$\boxed{- 8 \text{ Volt} = V_A - V_B}$$

$$V_A + IR = V_B$$

$$V_A - V_B = - IR$$

$$= - 2 \times 4$$

$$\boxed{= - 8 \text{ Volt}}$$

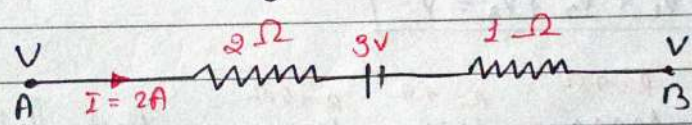


$$V_B + V - IR = V_A$$

$$\boxed{V - IR = V_A - V_B}$$

Q10
2016

The potential difference ($V_A - V_B$) b/w the points A and B in the given figure is.



- (A) -3V
 - (B) +3V
 - (C) +6V
 - (D) +9V ✓
- $$V_A - 2 \times 2 - 3 - 2 \times 1 = V_B$$
- $$V_A - 9V = V_B$$
- $$\boxed{V_A - V_B = 9 \text{ Volt}}$$

Q11 Value of the Resistance R in the figure is.

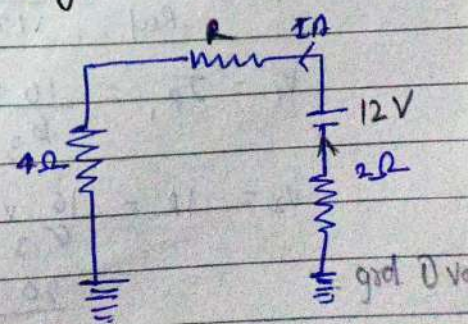
- (A) 6 Ohms ✓
- (B) 8 Ohms
- (C) 10 Ohms
- (D) 12 Ohms

$$0V - 1 \times 2 + 12 - 2R - 1 \times 4 = 0$$

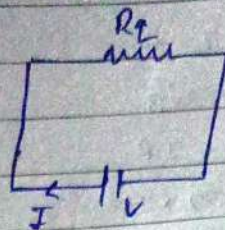
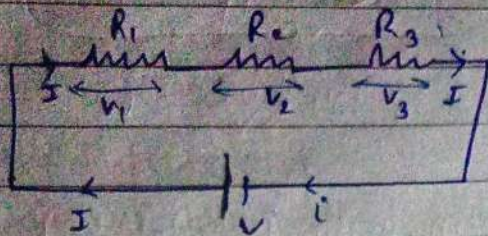
$$- 2 + 12 - R - 4 = 0$$

$$12 - 6 = R$$

$$\boxed{R = 6 \Omega}$$



Current remain Same Series Combination of Resistances



R is same
 $R_{eq} = nR$

$V = V_1 + V_2 + V_3$

$IR_1 + IR_2 + IR_3 = IR_{eq}$

$R_1 + R_2 + R_3 = R_{eq}$

↳ Law of Potential drop.

$V = IR$
 $V \propto R$

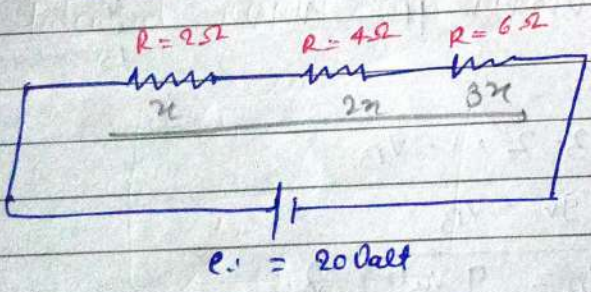
$\frac{V_1}{V_2} = \frac{R_1}{R_2}$

Current is same in all resistances in series combination

Sum of potential drop across each other resistance is potential of Battery.

$V_1 + V_2 + V_3 = V$

Ques



And Potential drop across each resistance

MR

$R_{eq} = 2 + 4 + 6 = 12 \Omega$

$I = \frac{V}{R_{eq}} = \frac{20}{12} = \frac{10}{6} \text{ A}$

$V_1 = IR_1 = \frac{10}{6} \times 2 = \frac{10}{3} \text{ V}$

$V_2 = IR_2 = \frac{10}{6} \times 4 = \frac{20}{3}$

$V_3 = \frac{10}{6} \times 6 = 10 \text{ V}$

$V = IR$

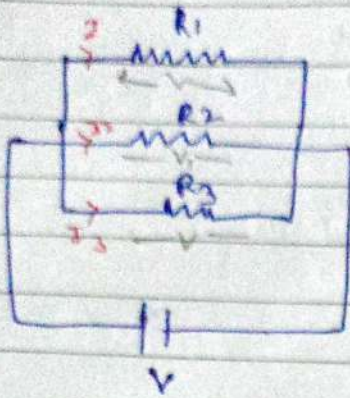
$6x = 20$

$x = \frac{20}{6} \text{ Volt}$

$(2x) = \frac{40}{6} \text{ Volt}$

$3x = 3 \left(\frac{20}{6} \right) = 10 \text{ V}$

Parallel Combination of resistances = $\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$



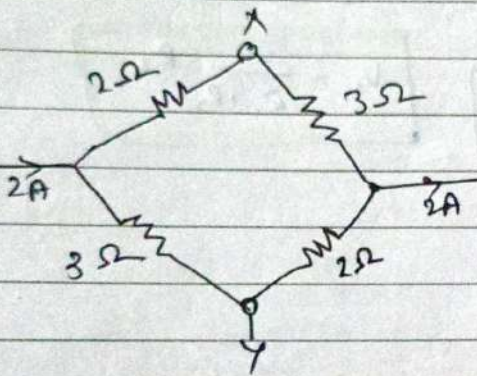
Potential drop across each resistances is same.

$$I = I_1 + I_2 + I_3$$

i all different in parallel

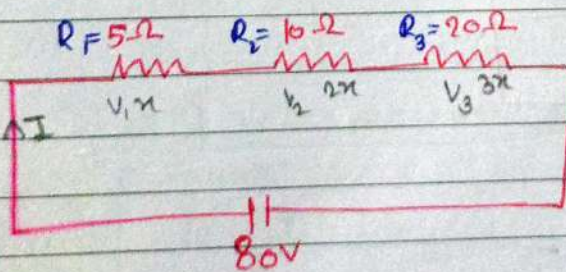
and V 's same

Find. ① -1 ② -1 ③ 2 ④ -2



Special

Find Current and Potential drop across each resistances



5Ω

$$x + 2x + 4x = 80$$

$$7x = 80$$

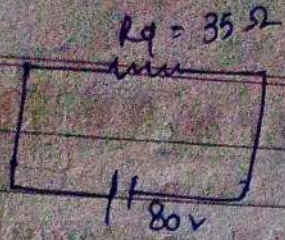
$$x = \frac{80}{7} \text{ Volt}$$

Potential drop in 10Ω

$$V_2 = 2x = \frac{160}{7} \text{ Volt}$$

$$V_3 = 4 \left(\frac{80}{7} \right) \text{ Volt}$$

Method

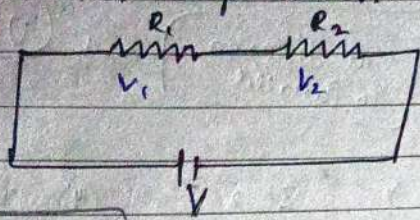


$$V_1 = IR = \frac{80 \times 8}{35}$$

$$= \frac{80}{7} \text{ A}$$

$$I = \frac{80}{35} \text{ Amp}$$

Ques Find Potential drop across R_1 and R_2



$$I = \frac{V}{R_{eq}} = \frac{V}{R_1 + R_2}$$

$$V_2 = IR_2$$

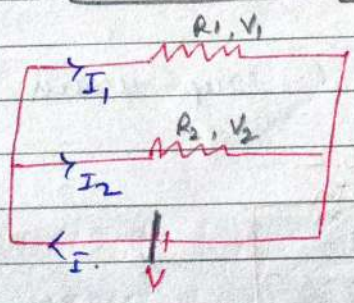
Formula

$$V_1 = IR_1 = \frac{V}{R_1 + R_2} R_1$$

$$V_2 = \frac{V}{R_1 + R_2} R_2$$

Parallel Combination

Potential across each resistor is same.



$$I = \frac{R_2}{R_1 + R_2} I$$

$$I = I_1 + I_2$$

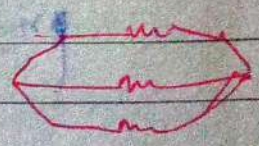
$$R_{eq} = \frac{R_1 R_2}{R_1 + R_2}$$

$$\frac{V}{R_q} = \frac{V_1}{R_1} + \frac{V_2}{R_2}$$

$$\frac{1}{R_q} = \frac{1}{R_1} + \frac{1}{R_2}$$

n - Identical resistances connected in parallel of each resistances if then $R_{eq} = ?$

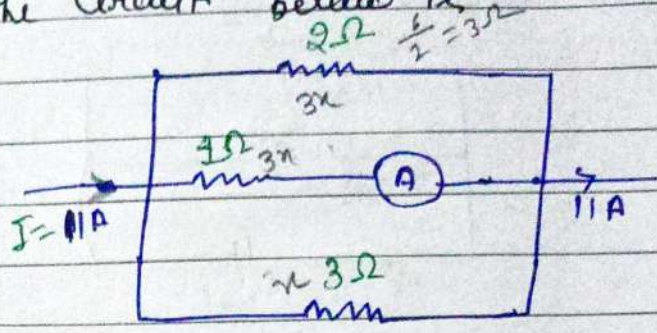
$$R_{eq} = \frac{R}{n}$$



The ammeter reading in the circuit below is

$I \propto \frac{1}{R}$

- Ⓐ 2A
 - Ⓑ 3A
 - Ⓒ 6A
 - Ⓓ 5A
- $R_{eq} = \frac{11}{6}$
- $I = 11A$
- $V = IR = \frac{11 \times 6}{1} = 6 \text{ Volt}$

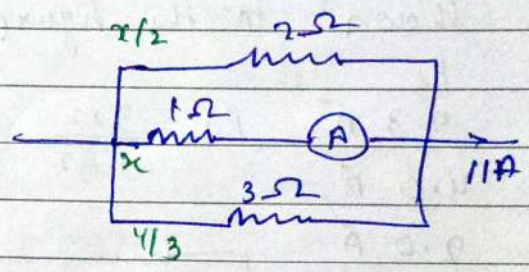


$\frac{1}{R_{eq}} = \frac{1}{1} + \frac{1}{2} + \frac{1}{3} = \frac{6+3+2}{6}$

$R_{eq} = \frac{6}{4} \Omega$

The ammeter reading in the circuit below is.

- Ⓐ 2A
 - Ⓑ 3A
 - Ⓒ 6A
 - Ⓓ 5A
- $\frac{x}{4} = \frac{2}{3}$
- $y = \frac{3x}{2}$
- $\frac{y}{2} + y + \frac{y}{3} = 11$
- $\frac{3y + 6y + 2y}{6} = 11$
- $\frac{11y}{6} = 11 \Rightarrow y = 6 \text{ Amp}$



$V = IR$

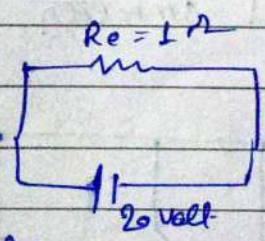
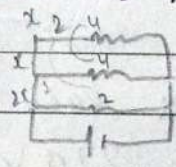
Same

$I \propto \frac{1}{R}$

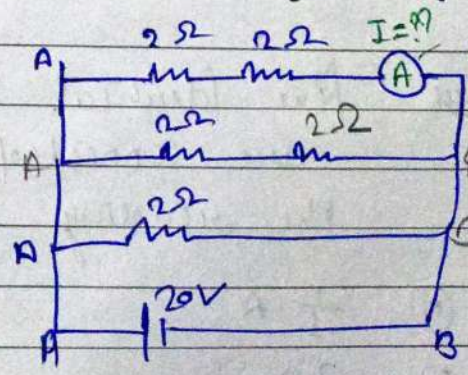
Current kha ganna.

The reading of the ammeter in the circuit below is

- Ⓐ 5A
 - Ⓑ 15A
 - Ⓒ 20A
 - Ⓓ 25A
- $4x = 20$
- $x = 5 \text{ Amp}$

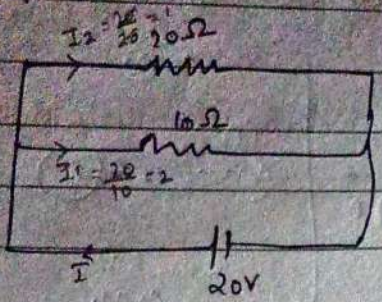


$I = \frac{20}{1} = 20 \text{ Amp}$



$I = \frac{20}{4} = 5 \text{ Amp}$

Q. And $I = ?$



2nd method

$$R_q = \frac{R_1 R_2}{R_1 + R_2} = \frac{20 \times 10}{20 + 10}$$

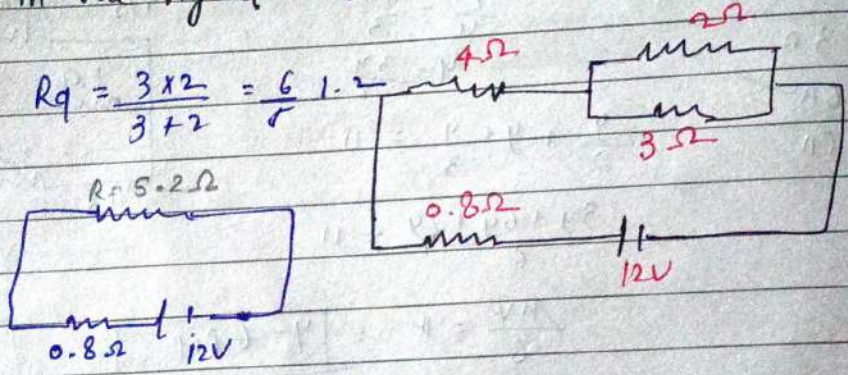
$$I = \left(\frac{V}{R_q} \right) = \frac{20}{20/3} = 3.6$$

$I = I_1 + I_2$
3 Amp

3 Amp

Q. A battery of 12V and an internal resistance of 0.8Ω is connected to 3 resistors as shown in the figure. The current i in the circuit

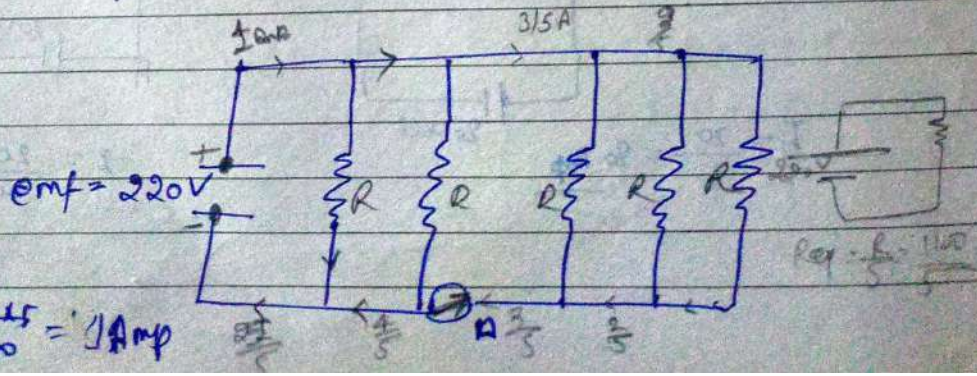
- (a) 2.3 A
- (b) 4.0 A
- (c) 2.0 A
- (d) 1.33 A



$$I = \frac{12 \text{ Volt}}{6} = 2 \text{ Amp}$$

Q. Five identical lamps each of resistance $R = 100 \Omega$ are connected to 220V as shown in the figure. The reading of ideal ammeter A is

- (a) $\frac{1}{5}$ A
- (b) $\frac{2}{5}$ A
- (c) $\frac{3}{5}$ A
- (d) 7 A



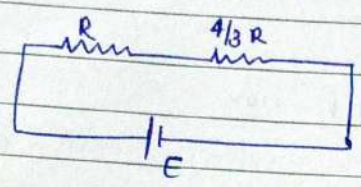
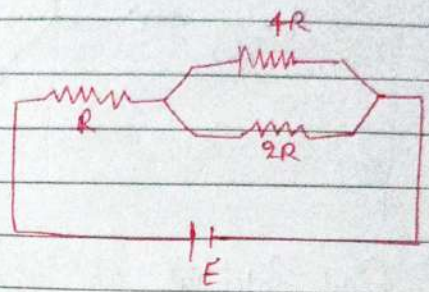
$$I = \frac{220 \times 5}{100} = 11 \text{ Amp}$$

Q. In a network as shown in the figure, the potential difference across the resistance $2R$ is (The cell has emf ϵ Volt and no internal resistance)

- (1) 2ϵ
- (2) $4\epsilon/7$
- (3) $\epsilon/7$
- (4) ϵ

$$R_{eq} = \frac{2R \times 4R}{2R + 4R}$$

$$R_{eq} = \frac{8R}{6} = \frac{4}{3}R$$



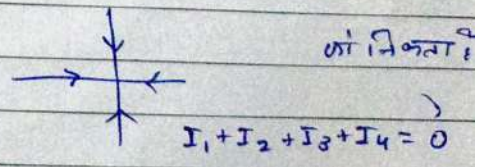
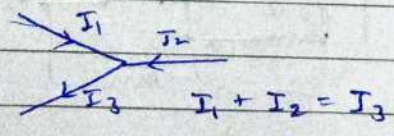
$$V = \frac{\frac{4}{3}R}{\frac{4}{3}R + R} E = \frac{\frac{4R}{3} E}{\frac{7R}{3}} = \frac{4E}{7}$$

Kirchoff's First Rule :- Junction Rule

At any junction, the sum of the currents entering the junction is equal to sum of currents leaving the junction

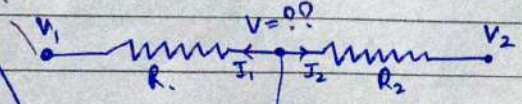
Explanation

When current are steady there is no accumulation of charges at any junction or at any point in a line therefore state of flow of charge into the junction is equal to state of flow of charge from the junction



Q. Find $V_{mid} = ?$
Point Potential

$$V_m = \frac{C_1 V_1 + C_2 V_2}{C_1 + C_2}$$



Point Rule

$$0 = I_1 + I_2$$

$$I_1 = -I_2$$

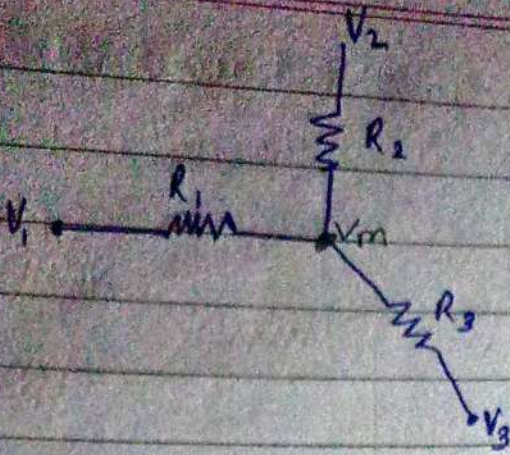
$$\left(\frac{V_m - V_1}{R_1} \right) = \left(\frac{V_m - V_2}{R_2} \right)$$

$$\frac{V_m - V_1}{R_1} = -\frac{V_m}{R_2} + \frac{V_2}{R_2}$$

$$\frac{V_m}{R_1} + \frac{V_m}{R_2} = \frac{V_1}{R_1} + \frac{V_2}{R_2}$$

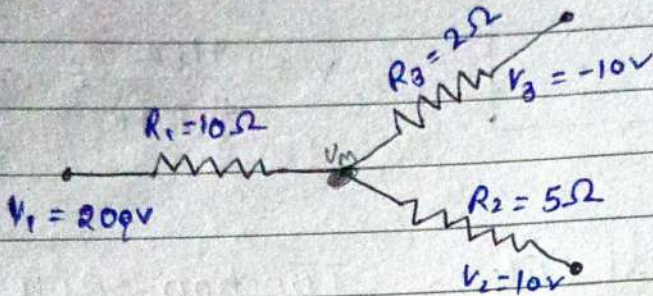
$$V_m \left(\frac{1}{R_1} + \frac{1}{R_2} \right) = \frac{V_1}{R_1} + \frac{V_2}{R_2}$$

$$V_m = \frac{\frac{V_1}{R_1} + \frac{V_2}{R_2}}{\left(\frac{1}{R_1} + \frac{1}{R_2} \right)}$$



$$V_m = \frac{\frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3}}{\left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}\right)}$$

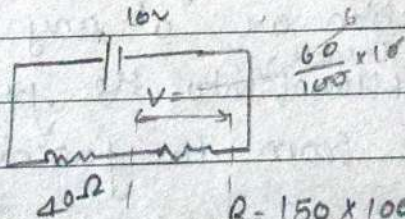
Find Potential at Junction.



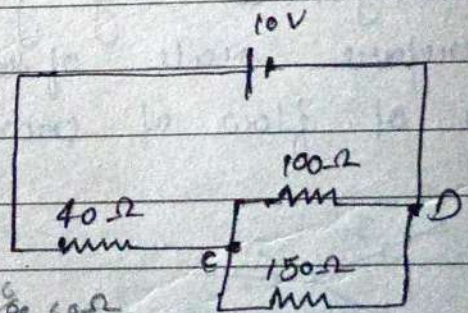
$$V_m = \frac{\frac{20}{10} + \frac{10}{5} - \frac{10}{2}}{\frac{1}{10} + \frac{1}{5} + \frac{1}{2}} = \frac{\frac{100 + 100 - 250}{50}}{\frac{5 + 10 + 25}{50}} = \frac{-50}{40} = -\frac{5}{4} = -1.25$$

In the network shown below, Potential difference across CD is

- a) 4V
- b) 6V ✓
- c) 10V
- d) 5V



$$R = \frac{150 \times 100}{150 + 100} = \frac{150 \times 100}{250} = \frac{300}{5} = 60 \Omega$$

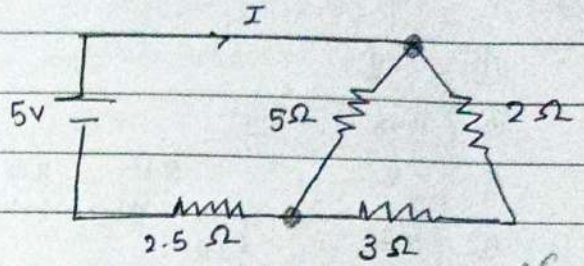
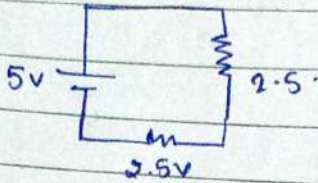


$$\frac{300}{5} = 60 \Omega$$

The current I through the cell in the network shown is

- (a) 3 A
- (b) 2 A
- (c) 1 A ✓
- (d) 4 A

$$I = \frac{5V}{5} = 1 \text{ Amp}$$



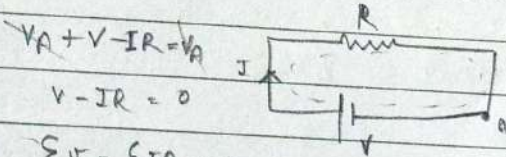
$$R = \frac{5 \times 5}{5 + 5} = \frac{25}{10} = 2.5 \Omega$$

KIRCHHOFF SECOND RULE LOOP RULE \rightarrow

Algebraic sum of changes in potential around any closed loop involving resistor and cells in the loop is zero.

Explanation :-

We know that electric ~~field~~ potential depend on the location of point. therefore starting with any point if we come back to the same point the total change of potential must be zero.

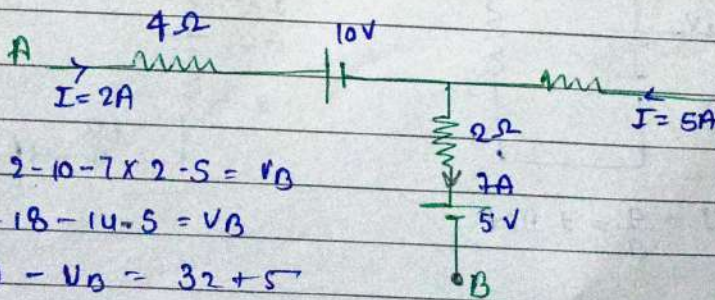


$$V_A + V - IR = V_B$$

$$V - IR = 0$$

sum $\Sigma V - EIR = 0$

find $V_A - V_B = ??$



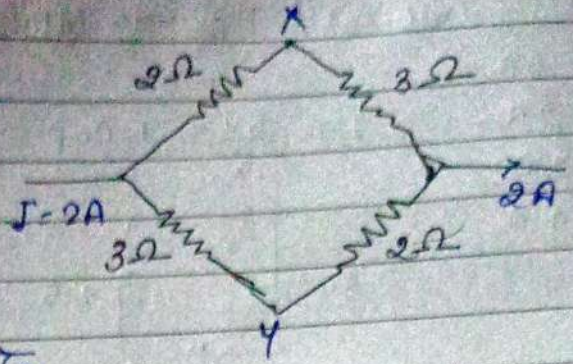
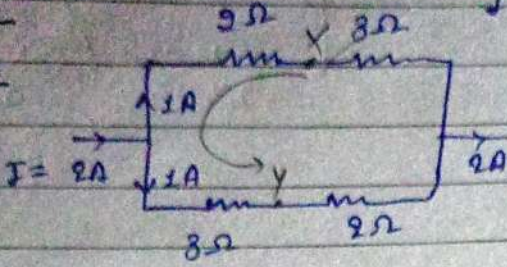
$$V_A - 4 \times 2 - 10 - 7 \times 2 - 5 = V_B$$

$$V_A - 18 - 14 - 5 = V_B$$

$$V_A - V_B = 32 + 5 = 37 \text{ Volt}$$

Ques Find $V_x - V_y = ?$

- Ⓐ 1
- Ⓑ -1
- Ⓒ 2
- Ⓓ -2



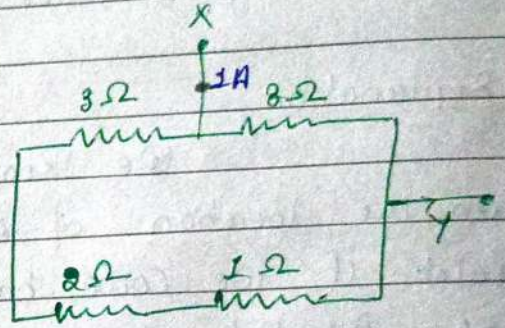
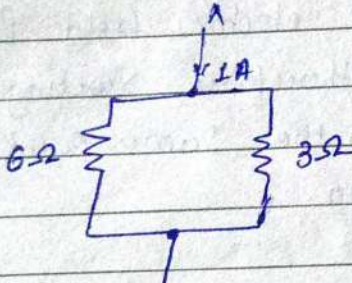
$$V_x + I_1 R_1 - I_2 R_2 = V_y$$

$$V_x + 2 \times 1 - 3 \times 1 = V_y$$

$$V_x - V_y = +3 - 2 = 1 \text{ Volt}$$

Ques find $V_x - V_y = ?$

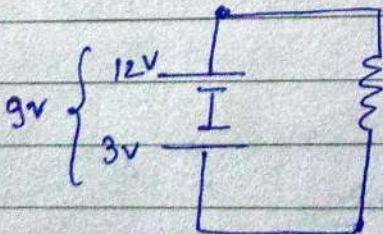
- Ⓐ 2
- Ⓑ 3
- Ⓒ 6
- Ⓓ 9



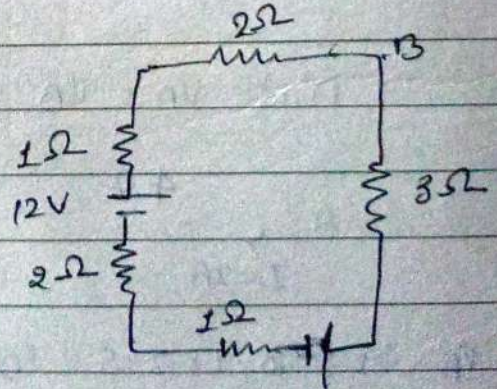
$$R_{eq} = \frac{6 \times 3}{6 + 3} = \frac{18}{9} = 2\Omega \quad V_x = 2 \times 1 = 2 \text{ Vol}$$

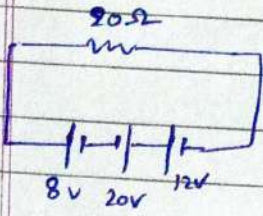
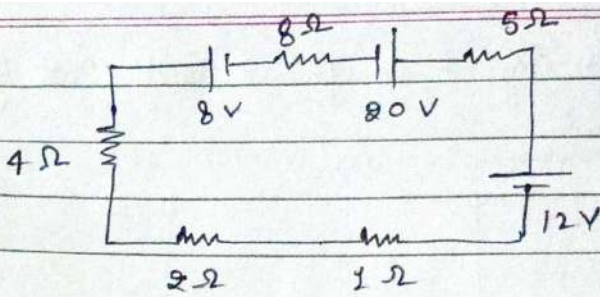
Ques Potential difference $V_B - V_A$ in the network shown in

- Ⓐ 7V ✓
- Ⓑ 6V
- Ⓒ 5V
- Ⓓ 8V



$$I = \frac{9}{9} = 1 \text{ Amp}$$





Potential difference $V_B - V_A$ in the network shown in

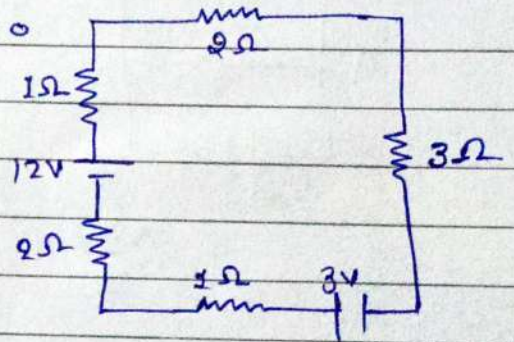
- ① 7V ✓
- ② 6V
- ③ 5V
- ④ 8V

$$-2I - 3I - 3 - I - 2I + 12 - I = 0$$

$$-9I + 9 = 0$$

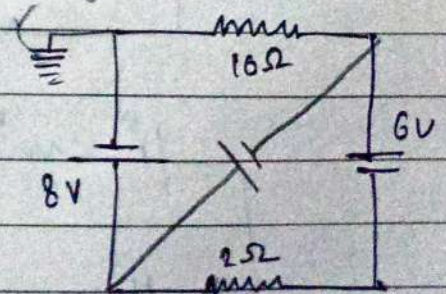
$$9 = 9I$$

$$I = \underline{1 \text{ Amp}}$$

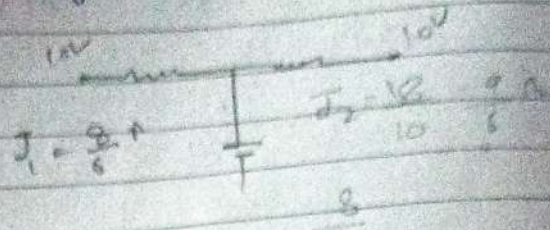
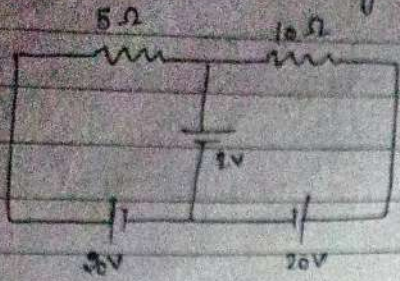


In the circuit shown in figure all cells are ideal. The current through 2 Ω resistor is *Potential drop 2V*

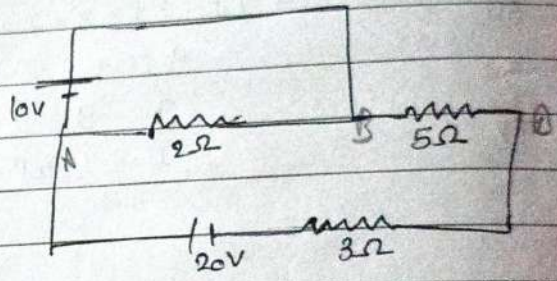
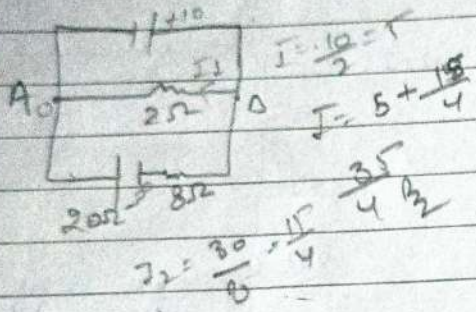
- 5 A
- 1 A ✓
- 0.2 A
- Zero



Find Current Passing through 2 Volt Battery??

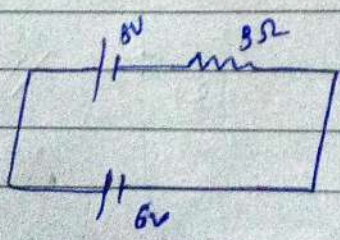
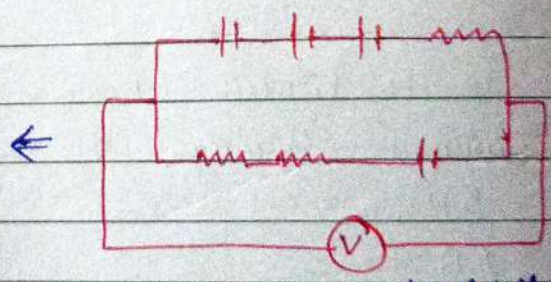
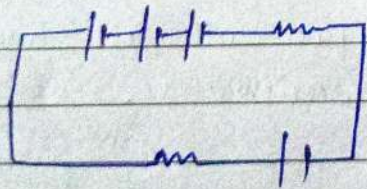


Find Current in given wire



Ques Reading of an ideal Voltmeter in the Circuit below is

- (a) Zero
- (b) 2V
- (c) 4V
- (d) 6V



$I = \frac{3}{3} = 1 \text{ Amp}$

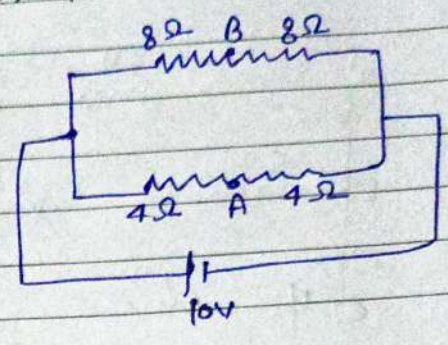
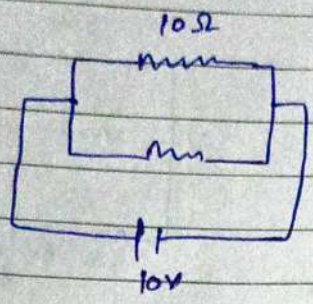
Ideal Voltmeter
R = Infinite
open wire

$V_A + 2 - 6 = V_B$

$V_A - V_B = +4 \text{ Volt}$

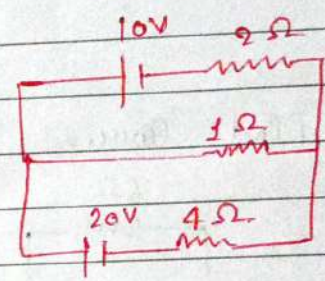
Ques The potential difference b/w points A and B is.

- ① $\frac{20}{7}$ V
- ② $\frac{20}{7}$ V
- ③ $\frac{10}{7}$ V
- ④ zero



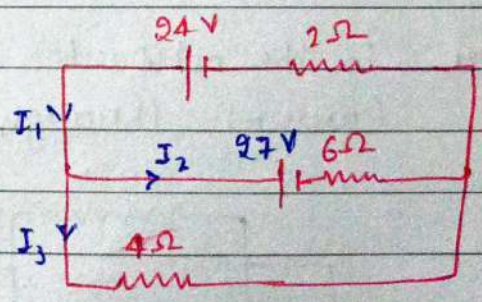
Ques The value of current through 2Ω resistor is.

- ① 1.0 A
- ② 1.5 A
- ③ 5.0 A
- ④ 2.1 A



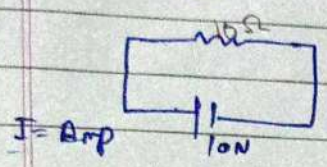
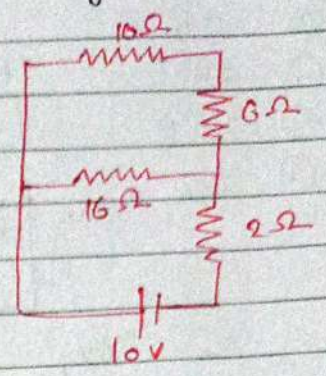
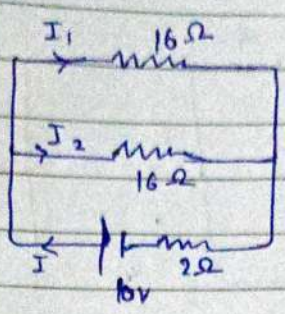
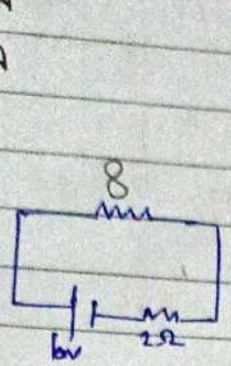
Ques In given circuit the value of currents I_1 , I_2 and I_3

- ① 3A, $\frac{3}{2}$ A, $\frac{9}{2}$
- ② $1\frac{9}{2}$ A, 3A, $\frac{3}{2}$ A
- ③ 5A, 4A, -3A
- ④ 7A, $\frac{5}{4}$ A, $\frac{9}{2}$ A



Ques Current I in the network shown in figure is.

- (1) 1 A
- (2) 0.5 A
- (3) 2 A
- (4) 5 A

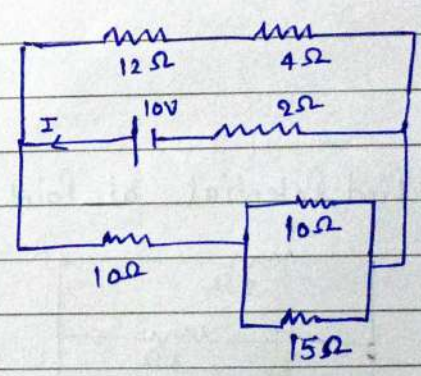
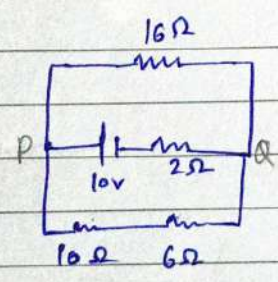
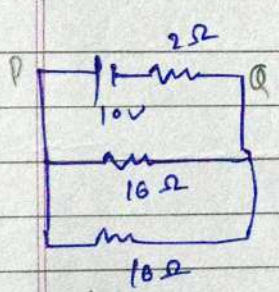
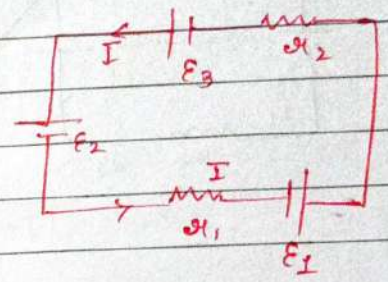


M-2

$$I \times r_2 + E_3 - E_2 - I \times r_1 + E_1 = 0$$

$$E_1 - E_2 + E_3 = I (r_1 + r_2)$$

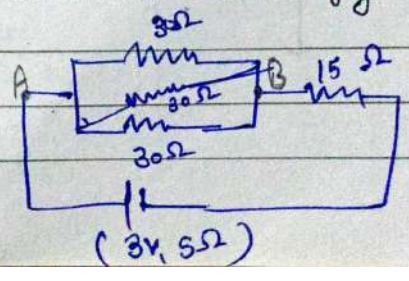
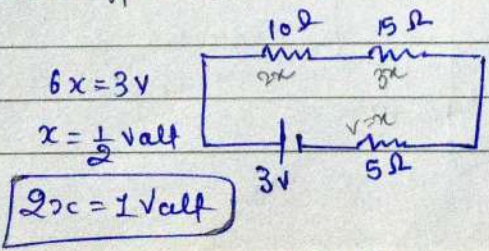
$$I = \frac{E_1 - E_2 + E_3}{r_1 + r_2}$$



$I = \frac{10}{10} = 1 \text{ Amp}$

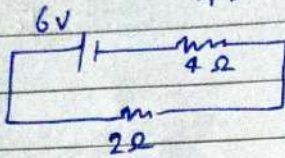
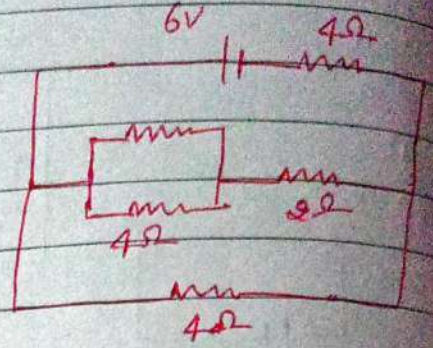
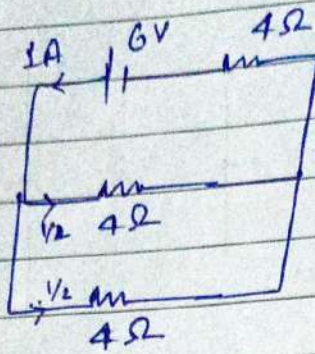
Ques Potential difference across AB in the network shown in figure is

- (a) 2V
- (b) 3V
- (c) 1V
- (d) 1.5V

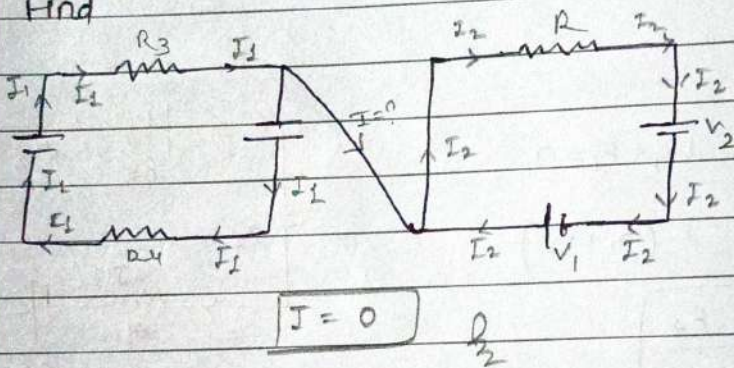


Ques The Current I in the Circuit shown below is

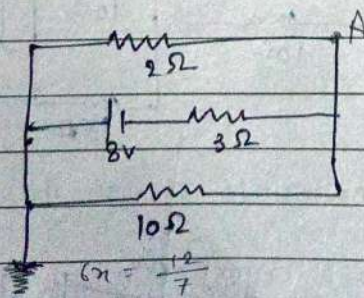
- (a) 1A
- (b) 2A
- (c) 0.5A
- (d) Zero



Q Find



Ques Find Potential at Point 'X'

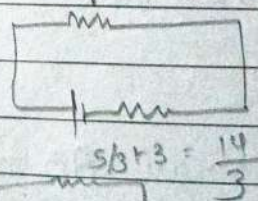


$$6V = \frac{12}{7}$$

$$I = \frac{2}{7} \text{ A}$$

$$V_x = 10 \times \frac{2}{7} = \frac{20}{7} \text{ V}$$

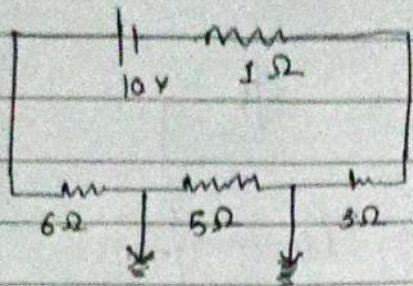
$$R = \frac{10 \times 2}{10 + 2} = \frac{20}{12} = \frac{5}{3} \Omega$$



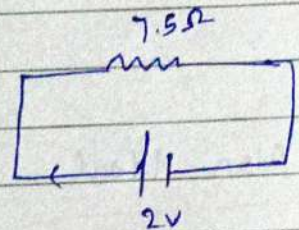
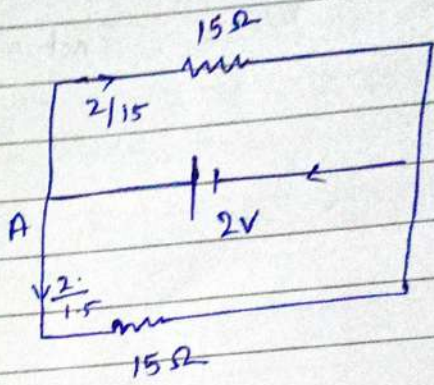
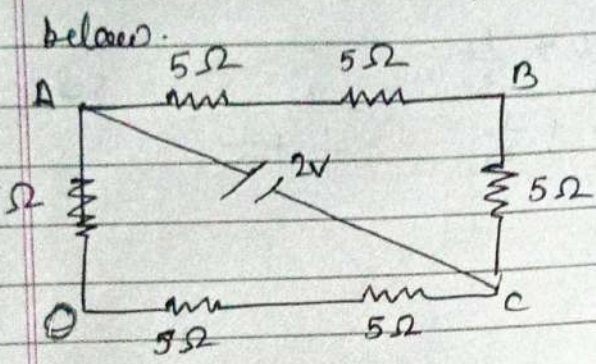
$$5/3 + 3 = \frac{14}{3}$$

$$I = \frac{8 \times 3}{14} = \frac{24}{14} = \frac{12}{7} \text{ A}$$

Find Current in the Circuit

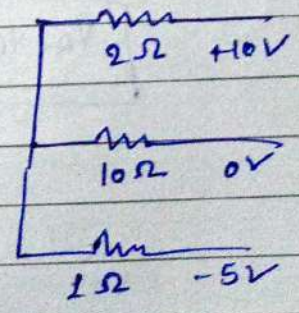
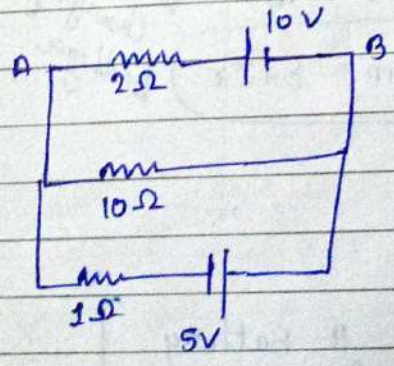
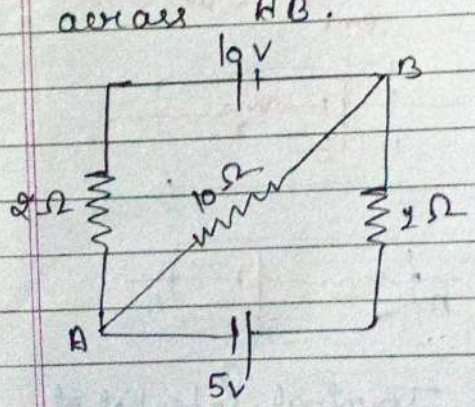


Find the Potential difference b/w Points B and B in the figure below.



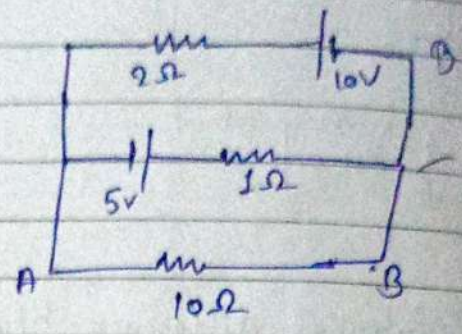
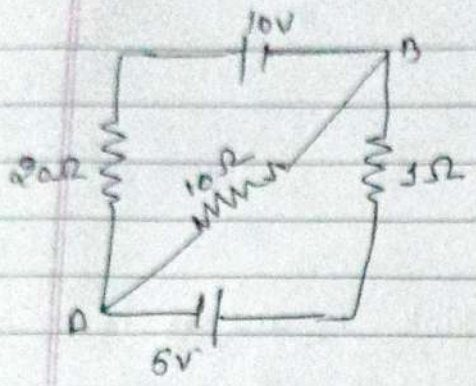
$$I = \frac{2V}{\left(\frac{15}{2}\right)} = \frac{4}{15} \text{ Amp.}$$

Find the Current through the 10Ω resistor connected across AB.



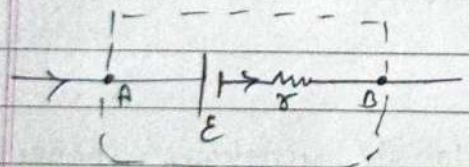
$$\frac{\frac{10}{2} - \frac{5}{1}}{\frac{1}{2} + \frac{1}{10} + \frac{1}{1}} = 0 \text{ across } 10\Omega$$

Ques Find the Current through the 10Ω resistance connected across AB.



$$\mathcal{E}_{net} = \frac{\mathcal{E}_1 + \mathcal{E}_2}{\frac{1}{r_1} + \frac{1}{r_2}} = \frac{10 - 5}{\frac{1}{2} + \frac{1}{1}} = 5 \text{ V}$$

Charging Battery

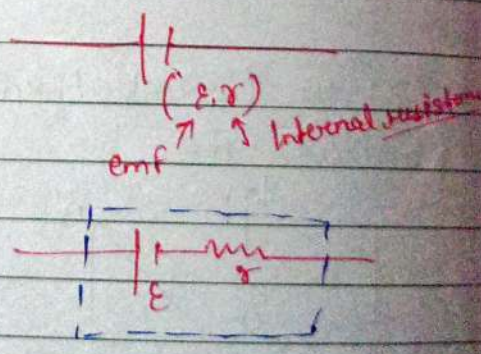


$$V_A - \mathcal{E} - Ir = V_B$$

$$V_A - V_B = V_{TP} = \mathcal{E} + Ir$$

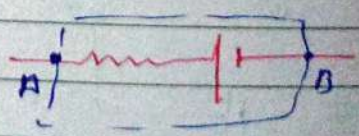
During charging battery.

Non-Ideal



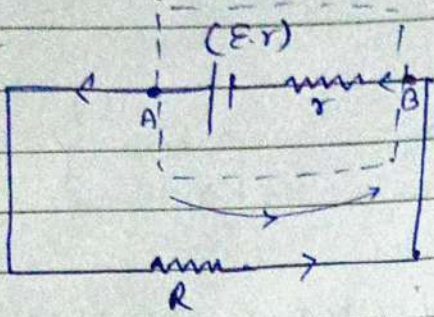
If Battery is not connected in any circuit $I = 0$

$$V_{AB} = \text{Terminal Potential of Battery} = \text{emf}$$



Discharging of battery

Terminal voltage during discharge



$$V_{TP} = \text{E.m.f} = \epsilon \times \text{No.}$$

$$V_A - \epsilon + I r = V_B$$

$$V_A - V_B = V_{TP} = \epsilon - I r$$

during discharge

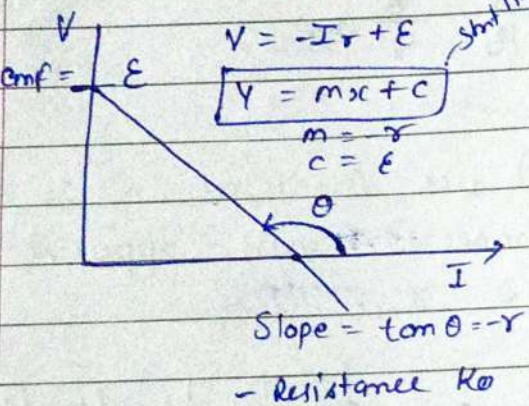
$$V = \epsilon - I r$$

Terminal potential diffⁿ across Battery during discharge

Graph b/w V (Terminal Potⁿ) B/w I

$$V = \epsilon - I r$$

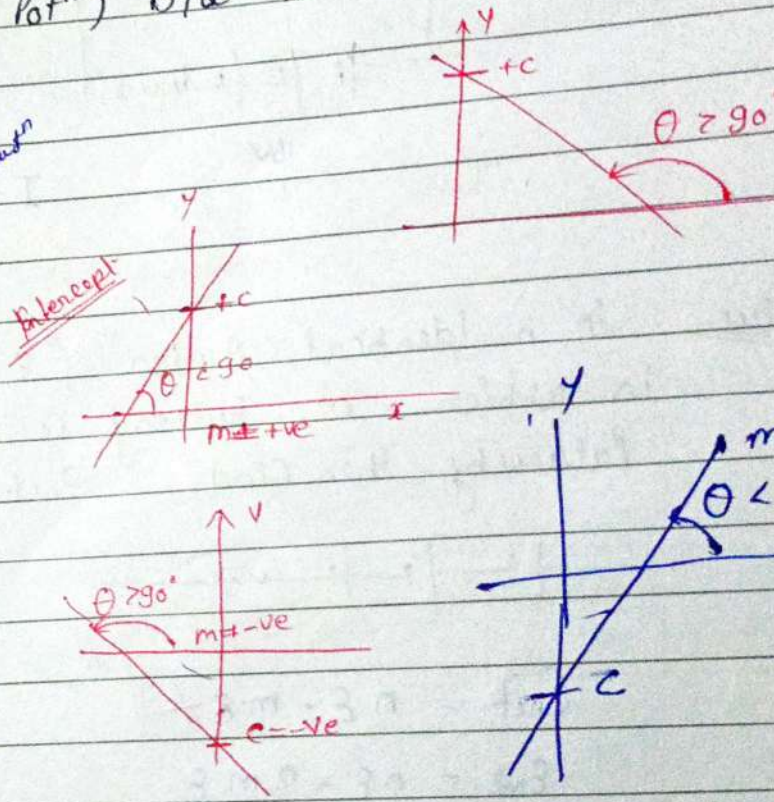
(const) (const)



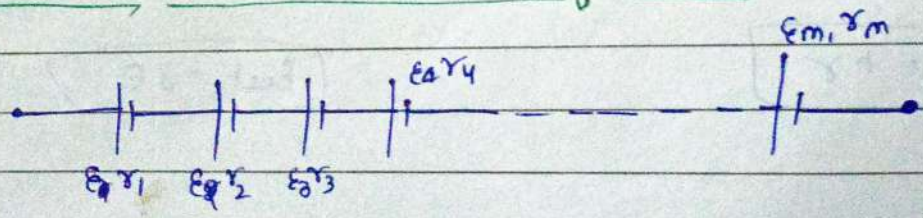
$$V = -I r + \epsilon$$

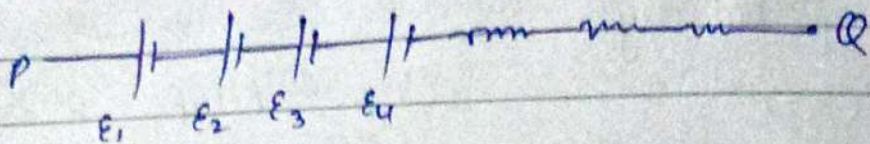
$$y = m x + c$$

$m = -r$
 $c = \epsilon$



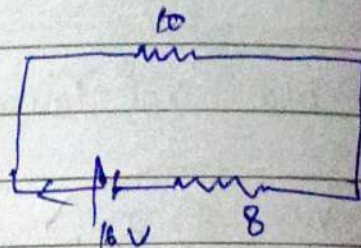
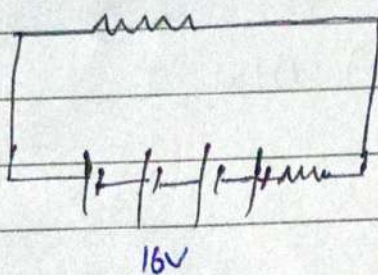
Series Combination of cell :->





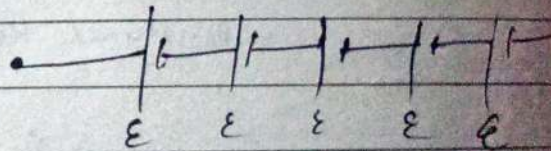
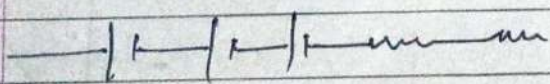
$$\left\{ \begin{array}{l} E_{net} = E_1 + E_2 + E_3 + E_4 + \dots + E_n \\ V_{in} = r_1 + r_2 + r_3 + r_4 + \dots + r_n \end{array} \right\}$$

Q. 4 - Identical Battery is connected in series of e.m.f. & internal resistance 2Ω through 10Ω external resistance then find current in external resist.



$$I = \frac{16}{18} = \frac{8}{9} \text{ Amp}$$

Q. In n-Identical Batter (E,r) are connected in series in which m battery is connected with opposite polarity then find E_{net} & r_{net}

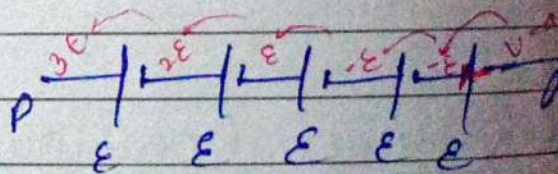


$$E_{net} = nE - mE$$

$$E_{net} = nE - 2mE$$

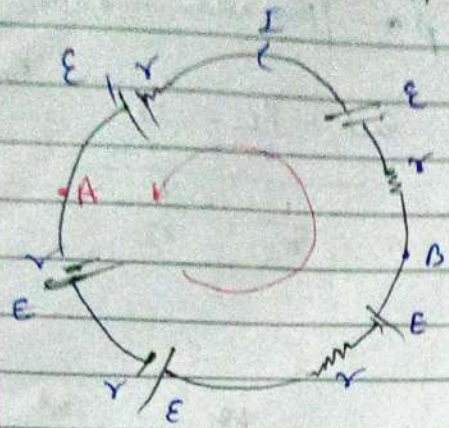
$$E_{net} = E(n - 2m)$$

$$r_{net} = nr$$



$$E_{net} = 3E$$

Find Potential diffⁿ b/w A & B



$$V_B - I r + E - I r + E = V_A$$

$$V_B - 2 I r + 2 E = V_A$$

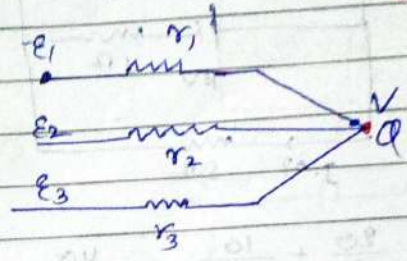
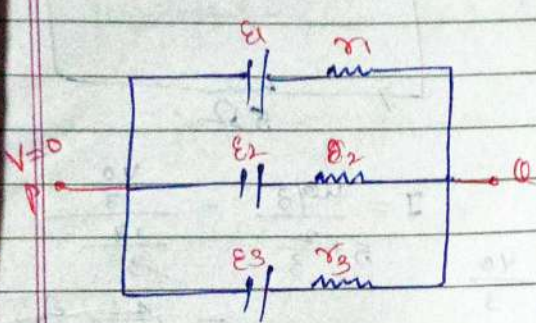
$$V_B - \frac{2 E r}{r} + 2 E = V_A$$

$$V_B = V_A$$

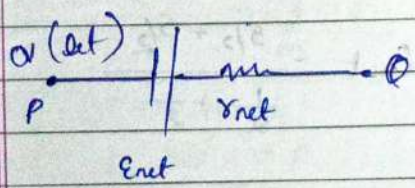
$$I = \frac{5E}{5r} = \frac{E}{r}$$

Parallel Combination of Cell :-

$$\frac{1}{r_{net}} = \frac{1}{r_1} + \frac{1}{r_2} + \frac{1}{r_3}$$

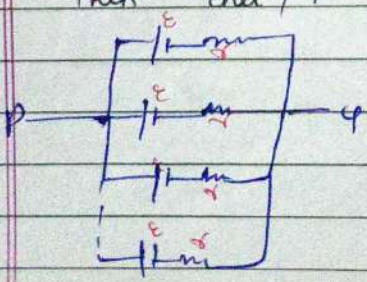


$$V_Q = \frac{\frac{E_1}{r_1} + \frac{E_2}{r_2} + \frac{E_3}{r_3}}{\frac{1}{r_1} + \frac{1}{r_2} + \frac{1}{r_3}}$$



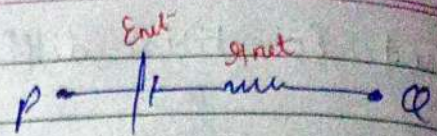
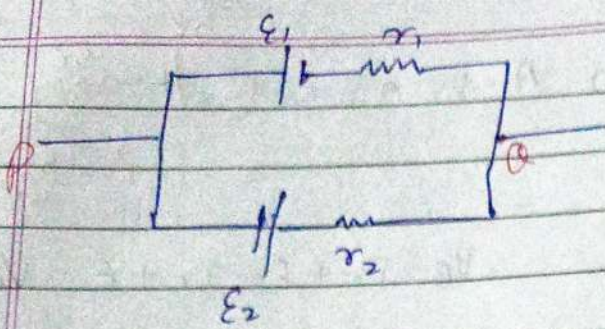
$$E_{net} = V_Q - V_P = \frac{\frac{E_1}{r_1} + \frac{E_2}{r_2} + \frac{E_3}{r_3}}{\frac{1}{r_1} + \frac{1}{r_2} + \frac{1}{r_3}}$$

Ex If n-Identical Battery (E, r) is connected in Parallel then Enet / r



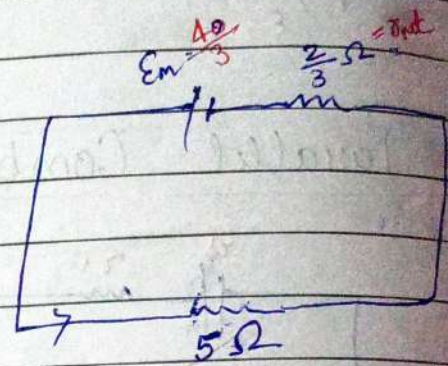
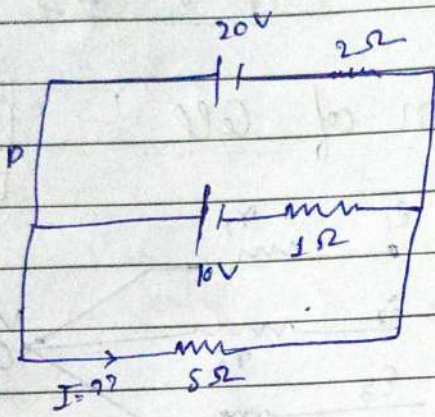
$$E_{net} = \frac{\frac{E}{r} + \frac{E}{r} + \frac{E}{r} + \dots + \frac{E}{r}}{\frac{1}{r} + \frac{1}{r} + \frac{1}{r} + \dots + \frac{1}{r}}$$

$$E_{net} = \frac{nE}{\frac{n}{r}} = E$$



$$E_{net} = \frac{E_1}{r_1} - \frac{E_2}{r_2} \div \left(\frac{1}{r_1} + \frac{1}{r_2} \right)$$

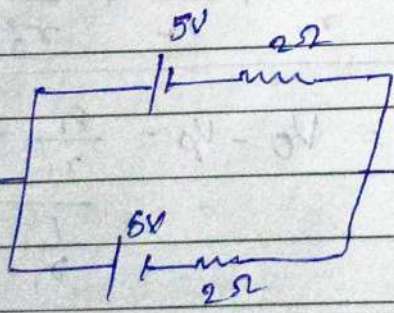
Ques Find Current in (5Ω)



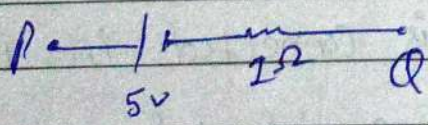
$$E_{net} = \frac{20}{2} + \frac{10}{1} = \frac{40}{2} = \frac{40}{3}$$

$$\frac{1}{2} + \frac{1}{1} = \frac{3}{2}$$

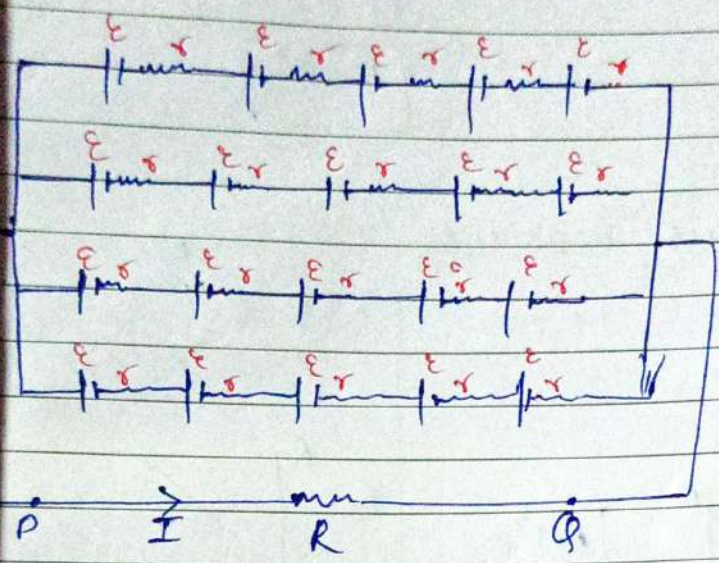
$$I = \frac{40/3}{5 + \frac{2}{3}} = \frac{40}{17}$$



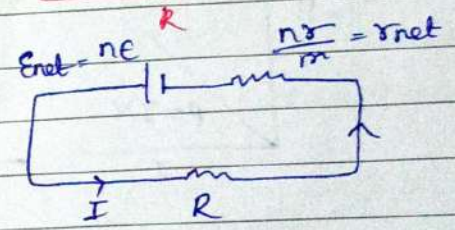
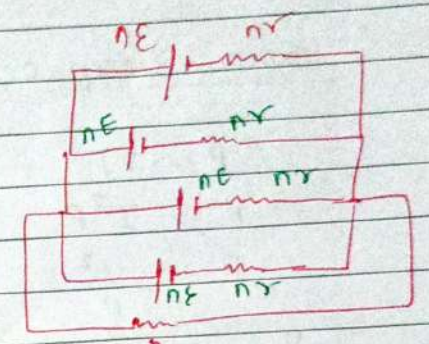
$$E_{net} = \frac{5/2 + 5/2}{\frac{1}{2} + \frac{1}{2}}$$



Mixed grouping of cell :- If n -Identical cells connected in series and m such combination connected in parallel then find E_{net} & r_{net} .



total cell = $n \times m$

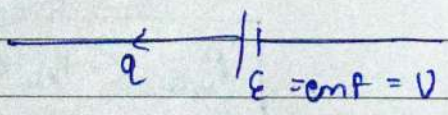


$$I = \frac{nE}{\frac{nr}{m} + R}$$

$$I = \frac{nE}{nr + mR}$$

$$I = \frac{nmE}{nr + mR}$$

Power Supply by the Battery

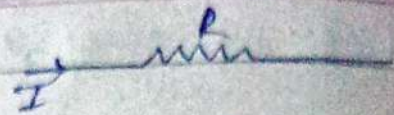


$$W = q \Delta V = qV$$

diffⁿ w.r.t time

$$P = \frac{dW}{dt} = V \frac{dQ}{dt}$$

$$P = IV$$



$$P = IV = I(IR)$$

$$P = I^2 R$$

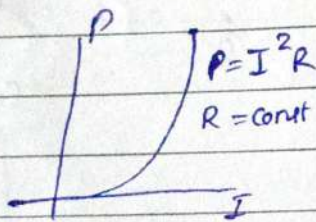
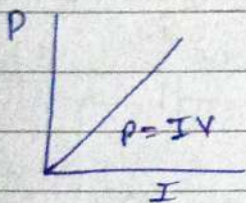
$$P = \frac{V^2}{R}$$

Power drop across resistance

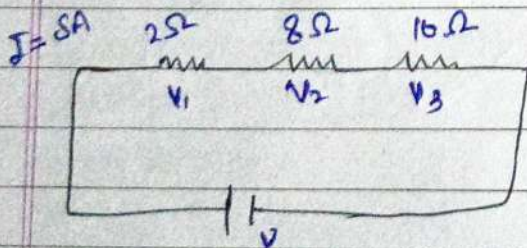
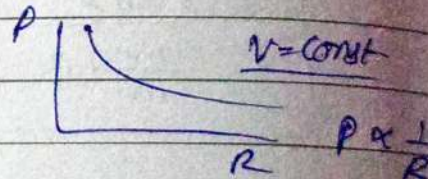
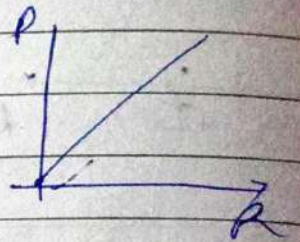
$$P = VI$$

$$P = I^2 R$$

$$P = \frac{V^2}{R}$$



$$P = I^2 R = \frac{V^2}{R}$$



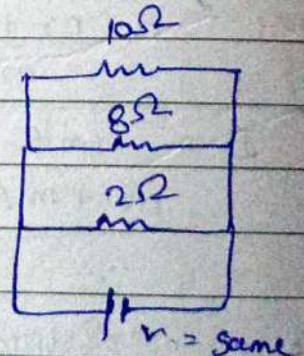
$$P \propto R$$

$$\frac{P_1}{P_2} = \frac{R_1}{R_2}$$

* In series combination

$$P_3 > P_2 > P_1$$

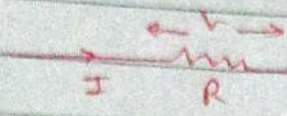
Ques



$$P \propto \frac{1}{R}$$

$$P_{10\Omega} < P_{8\Omega} < P_{2\Omega}$$

Joule Law of heating effect



$$P = VI = I^2 R = \frac{V^2}{R}$$

Heat law Per-sec

$$\frac{dH}{dt} = I^2 R$$

M (Heat loss) $\propto I^2$
 $H \propto R$
 $H \propto t$

$$\left. \begin{aligned} H &= I^2 R t \\ H &= \frac{V^2}{R} t \\ H &= V I t \end{aligned} \right\}$$

$I = \text{Variable}$

$$H = R \int I^2 dt$$

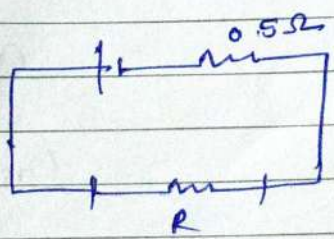
$I = \text{const}$

$$H = I^2 R t$$

Ques

A battery of e.m.f 10 v and internal resistance 0.5Ω is connected across a variable resistance R . The value of R which the power delivered in it is maximum is given by.

- ① 0.5Ω
- ② 1.0Ω
- ③ 2.0Ω
- ④ 0.25Ω

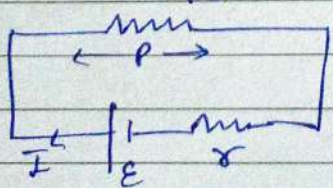


Maximum Power H^m

$$r_{in} = R$$

Maximum Power theorem

$R \leftarrow$ Variable External load Resistance



$$P = I^2 R$$

$$P = \left(\frac{E}{R+r} \right)^2 R$$

Power supply by the battery to the external resistance will be max^m when value of external $R=r$

$$I = \frac{E}{R+r}$$

$$P = \frac{E^2 R}{(R+r)^2}$$

$$P_{max} = \frac{E^2 R}{4R^2} = \frac{E^2}{4R}$$

Power drop across 'R' Resistance

Power drop P will be max^m when $\frac{dP}{dR} = 0$

$$P = \frac{\epsilon^2 R}{(R+\gamma)^2} \quad (\epsilon \text{ and } \gamma \text{ are const)}$$

$$\left(\frac{dP}{dR}\right) = 0 = \epsilon^2 \frac{d}{dR} \frac{R}{(R+\gamma)^2}$$

$$0 = \frac{d \left(\frac{R}{(R+\gamma)^2} \right)}{dR} = \frac{(R+\gamma)^2 \frac{dR}{dR} - R \cdot 2(R+\gamma)}{(R+\gamma)^{2 \times 2}}$$

$$R + \gamma = 2R$$

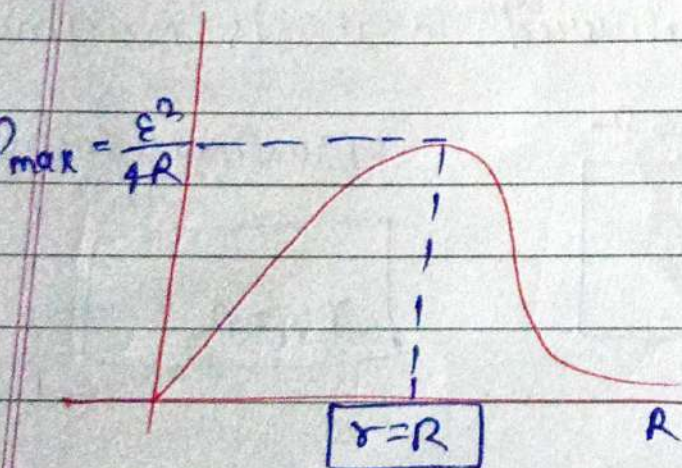
$$\gamma = 2R - R = R$$

$$\boxed{\gamma = R} \quad \text{h}$$

$$(R+\gamma)^2 - R \cdot 2(R+\gamma) \cdot (1) = 0$$

$$\cancel{(R+\gamma)^2} = 2R \cancel{(R+\gamma)}$$

Power graph b/w P and R



$$P = \frac{\epsilon^2 R}{(R+\gamma)^2}$$

Case-1 $R=0 \rightarrow P=0$

Case-2

$$R \ll \ll \gamma$$

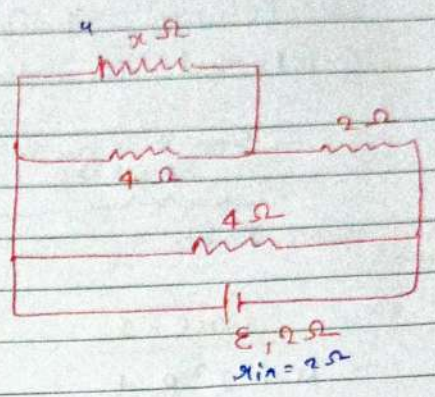
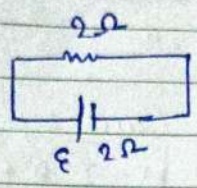
$$P = \frac{\epsilon^2 R}{\gamma^2} \propto R$$

Case-3

$$R \gg \gg \gamma$$

Find x so that power loss will be maximum in external circuit.

- 9 Ω
- 4 Ω
- 8 Ω
- 3 Ω



Find R so that power supplied by the battery is maximum

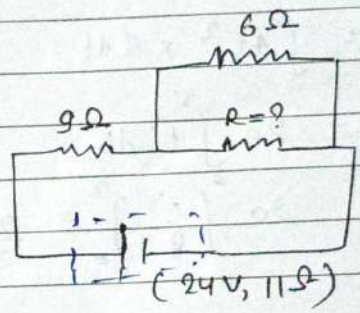
$$\frac{G \times R}{G + R} = 2$$

$$6R = 12 + 2R$$

$$6R - 2R = 12$$

$$4R = 12$$

$$\boxed{R = 3\Omega}$$



Current 2 A is flowing through a conductor of resistance 4 Ω find the electrical energy consumed in 10 s.

$I = 2 \text{ Amp}$

$$H = I^2 R t$$

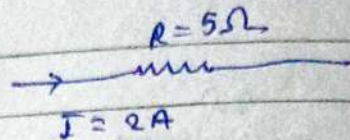
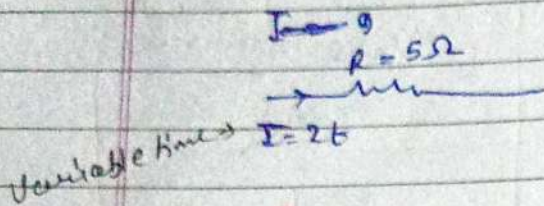
$$(2)^2 \times 4 \times 10$$

$$4 \times 4 \times 10$$

$$\boxed{H = 160 \text{ J}}$$

* Current 2 A is flowing through a conductor of resistance 4Ω . Find the electrical energy consumed in 10 s .

Q. Find heat loss in both case.



Case - 1

$$H = I^2 R t$$

$$dH = I^2 R dt$$

$$\int dH = \int 4t^2 \times 5 dt$$

$$\text{Heat} = 20 \int_0^2 t^2 dt =$$

$$20 \left[\frac{t^3}{3} \right]_0^2 = \frac{20 \times 8}{3} = \frac{160}{3} \text{ J}$$

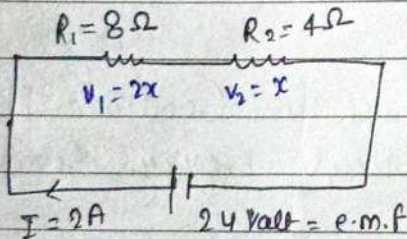
Case - 2

$$H = I^2 R t$$

$$(2)^2 \times 5 \times 2$$

$$4 \times 10 = 40 \text{ J}$$

Q.4



Find power loss in each resistance

(i) Power loss

$$P_{\text{net loss}} = P_1 + P_2$$

$$P_{\text{net}} = I^2 R_{\text{eq}} = (2)^2 \times 12$$

$$\boxed{48 \text{ W}}$$

(ii) $P_{\text{total}} = \frac{V^2}{R_{\text{eq}}}$

$$\frac{24 \times 24}{12} = \boxed{48 \text{ W}}$$

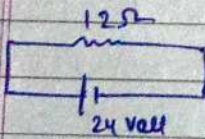
(iv)

Method - 1

$$P_{\text{total}} = I^2 R$$

$$4 \times (2)^2 \times 4 = 16 \text{ W}$$

$$\boxed{\text{total power} = 48 \text{ W}}$$



$$I = \frac{24}{12} = 2$$

$$\boxed{I = 2 \text{ amp}}$$

$$P_{\text{loss}} = I^2 R$$

$$8 \times (2)^2 \times 8$$

$$4 \times 8 = 32 \text{ W}$$

Power balance = $P_1 + P_2$

$P_{total} = I^2 R_{eq} = \frac{(12)^2}{4} \times 12$
 $4 \times 12 = 48 \text{ Watt}$

Method - 4

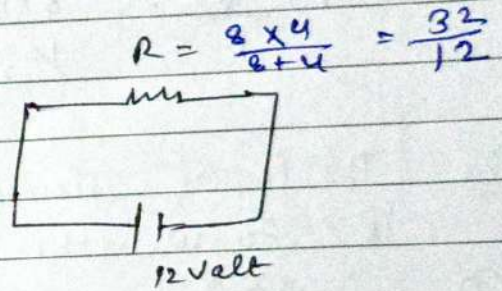
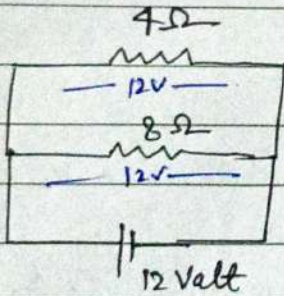
$x + 2x = 24$

$3x = 24$

$x = 8 \text{ Volt}$

$P_{4\Omega} = \frac{(8)^2}{4} = 16 \text{ W}$

$P_{8\Omega} = \frac{16 \times 16^2}{16} = 32 \text{ W}$

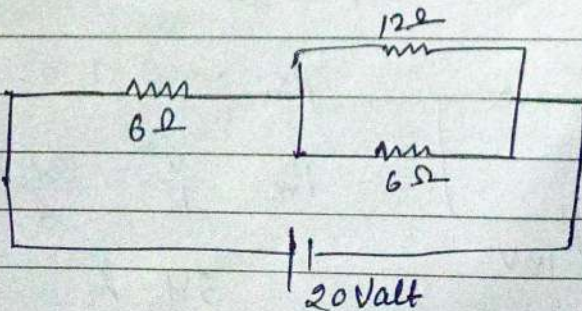


Power in $4\Omega = \frac{12 \times 12^3}{4} = 36 \text{ W}$

Power in $8\Omega = \frac{12 \times 12^3}{8} = 18 \text{ W}$

$P_{net} = \frac{V^2}{R_{eq}} = \frac{12 \times 12}{\frac{32}{12}}$
 $\frac{12 \times 12 \times 12 \times 3}{32}$
 $18 \times 3 = 54 \text{ W}$

$P_{total} = (18 + 36)$
54 Watt



Find Power loss in 12Ω Resistance?

Ques Power dissipated across the $8\ \Omega$ resistor in the circuit shown here is 2 watt, the power dissipated in watt Ohm across the $3\ \Omega$ resistor is

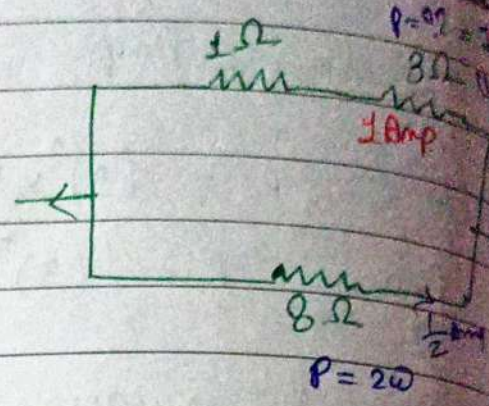
- 18
- ① 3.0
- ② 2.0
- ③ 1.0
- ④ 0.5

$$I^2 = \frac{1}{4}$$

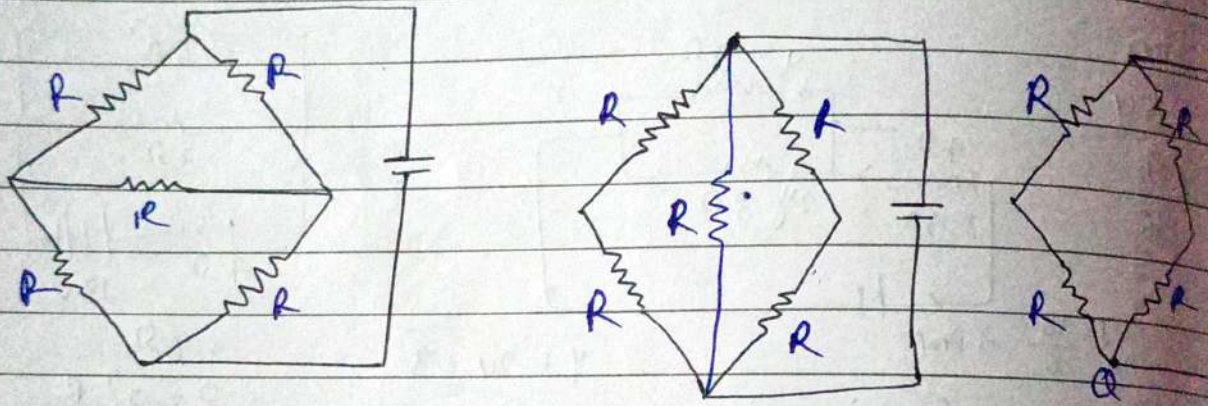
$$I = \frac{1}{2} \text{ Amp}$$

$$P = I^2 R$$

$$P = \frac{1}{4} \times 8$$

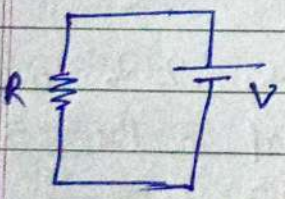


Ques
2008



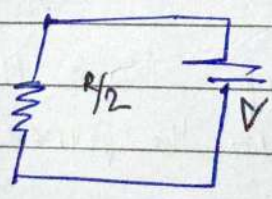
If all 5-resistances are identical then compare power in each case

Case-1



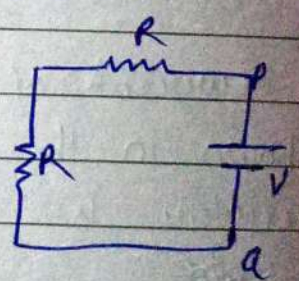
$$P_1 = \frac{V^2}{R}$$

Case-2



$$P_2 = \frac{2V^2}{R}$$

Case-3

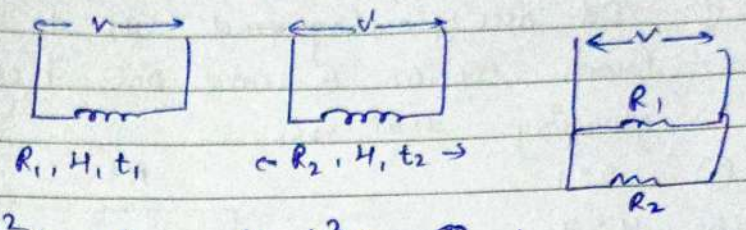


$$P_3 = \frac{V^2}{2R}$$

$$P_2 > P_1 > P_3$$

A heater boils certain amount of water in 15 minutes. Another heater boils same amount of water in 10 minutes. Time taken to boil same amount of water when both are used in parallel is,

- a) 25 minutes
- b) 6 minutes
- c) 12 minutes
- d) 12.5 minutes



$$H = \frac{V^2}{R_1} t_1 \quad \text{--- (I)}$$

$$H = \frac{V^2}{R_2} t_2 \quad \text{--- (II)}$$

$$H = \frac{V^2}{R_{eq}} t_0, \quad H = V^2 t \left(\frac{1}{R_{eq}} \right) = t^2 \left(\frac{1}{R_1} + \frac{1}{R_2} \right)$$

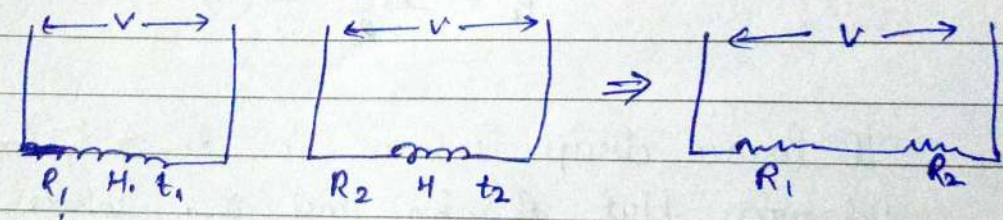
$$t = \frac{t_1 t_2}{t_1 + t_2} = \frac{15 \times 10}{15 + 10} = \frac{150}{25} = 6 \text{ min}$$

$$H = \frac{V^2 t}{R_1} + \frac{V^2 t}{R_2}$$

$$H = \frac{H t}{t_1} + \frac{H t}{t_2} = t = \left(\frac{1}{t_1} + \frac{1}{t_2} \right) t = \frac{1}{\frac{1}{t_1} + \frac{1}{t_2}}$$

Two heater coil separately take 10 minutes and 5 minutes to boil certain amount of water. If both the coils are connected in series, the time taken will be.

- a) 15 min
- b) 4.5 min
- c) 3.33 min
- d) 2.5 min



$$H = \frac{V^2}{R_1} t_1$$

$$H = \frac{V^2}{R_2} t_2$$

$$H = \frac{V^2}{R_{eq}} t = \frac{t^2}{R_1 + R_2}$$

$$R_1 = \frac{V^2 t_1}{H}$$

$$\frac{V^2 t}{H} = \frac{V^2 t_1}{H} + \frac{V^2 t_2}{H}$$

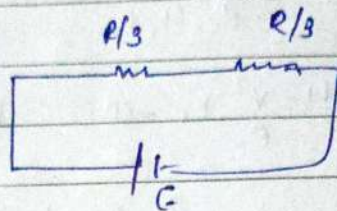
$$H = \frac{H t}{t_1 + t_2}$$

$$t = t_1 + t_2$$

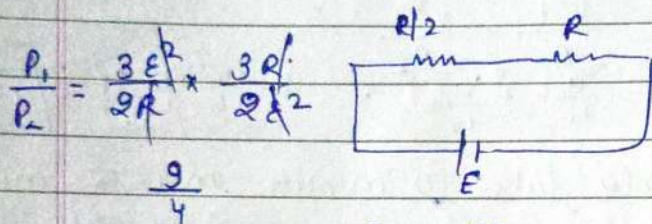
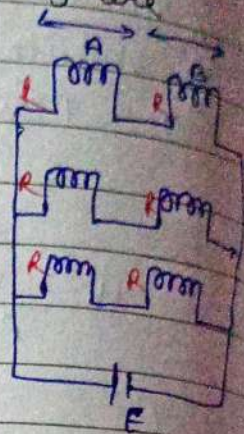
Ques Six similar bulbs are connected as shown in the figure with a DC source of emf, and zero internal resistance. The ratio of power consumption by the bulbs when

- (i) All are glowing and (ii) In the situation when two from section A and one from section B are glowing will be.

- (a) 9:1
 (b) 4:9
 (c) 9:4 ✓
 (d) 1:2



$$P_1 = \frac{3E^2}{2R} \quad \text{--- (i)}$$



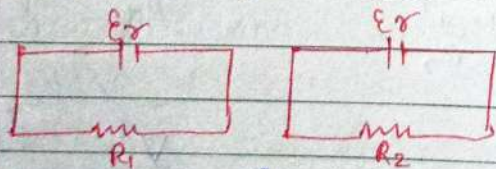
$$\frac{P_1}{P_2} = \frac{3E^2}{2R} \times \frac{3R}{2R^2}$$

$$\frac{9}{4}$$

$$R_1 = \frac{3R}{2}$$

$$P_2 = \frac{2E^2}{2R} \quad \text{--- (ii)}$$

Ques If power drop is same in R_1 and R_2 then find relation b/w R_1 , R_2 and r , where battery is same in both case.



$$P_1 = I^2 R_1 = \left(\frac{E}{R_1 + r} \right)^2 R_1$$

$$P_2 = \left(\frac{E}{R_2 + r} \right)^2 R_2$$

$$P_1 = P_2$$

$$\frac{E^2}{(R_1 + r)^2} R_1 = \frac{E^2}{(R_2 + r)^2} R_2$$

$$\frac{R_1}{(R_1 + r)^2} = \frac{R_2}{(R_2 + r)^2}$$

$$R_1 (R_1 + r)^2 = R_2 (R_2 + r)^2$$

$$\sqrt{R_1} (R_1 + r) = \sqrt{R_2} (R_2 + r)$$

$$R_1 \sqrt{R_1} + \sqrt{R_1} r = R_2 \sqrt{R_2} + \sqrt{R_2} r$$

$$\boxed{r = \sqrt{R_1 R_2}}$$

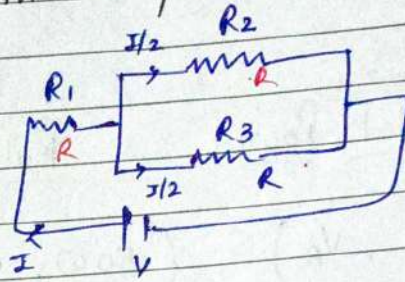
Three identical resistors $R_1 = R_2 = R_3$ are connected as shown to a battery of constant e.m.f. The power dissipated is,

(1) the least in R_1

(2) greatest in R_1 ✓

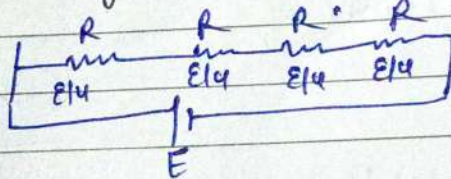
(3) in the ratio 1:2 in resistances R_1 and R_2 respectively

(4) The same in R_1 and in the parallel combination of R_2 and R_3 .



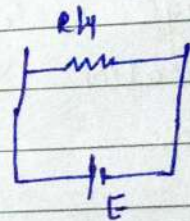
Four equal resistances dissipate 5 W power together when connected in series to a battery of negligible internal resistance. The total power dissipated in these resistances when connected in parallel across the same battery would be.

- (1) 125 W
- (2) 80 W
- (3) 20 W
- (4) 5 W



$$R_{eq} = 4R$$

$$P = \frac{E^2}{4R} = 5 \text{ Watt}$$



$$P' = \frac{4E^2}{R} = 4 [20W] = 80W$$

An electric kettle takes 4 A current at 220 V. How much time will it take to boil 1 Kg of water from temperature 20°C ? The temp of boiling water is

- 1. 4.2 min
- 2. 6.3 min
- 3. 8.4 min
- (4) 12.6 min. ✓

$$T_1 = 20^\circ\text{C}$$

$$T_2 = 100^\circ\text{C}$$

$$m = 1000\text{ gm}$$

$$H = IVt = ms\Delta T$$

$$t_{in} = \frac{ms\Delta T}{IV} = \frac{1000 \times 4.2 \times 80}{11 \times 220^2}$$

$$S = 1\text{ cal/gm}^\circ\text{C} = \frac{4.2\text{ J}}{10^{-3}\text{ kg}^\circ\text{C}}$$

$$= 4.2 \times 10^3\text{ J/kg}$$

$$\text{time} = \frac{4.2 \times 10^3}{11}$$

{ Rated Power & Rated Voltage }

$$(P_R, V_R) = (50\text{ W}, 220\text{ V})$$

Bulb is pure Resistance

$$P_R = \frac{V_R^2}{R_{\text{Bulb}}}$$

Rated Power and Rated Voltage only given to Calculate Resistance of Bulb.

$$R_{\text{Bulb}} = \frac{V_R^2}{P_{\text{Rated}}}$$

BOIB

⇒ Pure Resistance

P_R, V_R ← Rated Power, Rated Voltage

$$P_R = \frac{V_R^2}{R_{\text{Bulb}}}$$

$$R_{\text{Bulb}} = \frac{V_R^2}{P_{\text{Rated}}}$$

Rated Power and Rated Voltage only given to Calculate Resistance to Bulb.

$$P_{\text{consumed}} = \left(\frac{V_s}{V_R}\right)^2 P_{\text{Rated}}$$

$R \propto \frac{1}{P}$

Two bulbs are of (40 W, 200V) and (100 W, 200 V). Then correct relation for their resistance is.

(a) $R_{40} < R_{100}$

(b) $R_{40} > R_{100}$ ✓

(c) $R_{40} = R_{100}$

(d) No relation can be predicted

An electric bulb is rated 60 W, 220 V. The resistance of its filament is.

(a) 870Ω

(b) 780Ω

(c) 708Ω

(d) 807Ω

$$R = \frac{V_R^2}{P_R} = \frac{220 \times 220}{60} = \frac{220 \times 11}{3}$$

When three identical bulbs of 60 watt, 200 Volt rating are connected in series to a 200 Volt supply.

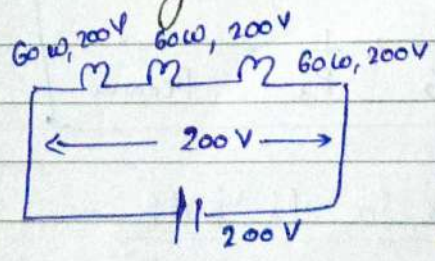
The power drawn by them will be

(a) 60 watt

(b) 180 watt

(c) 10 watt

(d) 20 watt



$$\frac{1}{P_c} = \frac{1}{60} + \frac{1}{60} + \frac{1}{60} = \frac{3}{60}$$

$$\frac{1}{P_c} = \frac{1}{20}$$

$$P_c = 20W$$

$$P_{one\ bulb} = \left(\frac{V_s}{V_R}\right)^2 P_R = \left(\frac{1}{3}\right)^2 \times 60W$$

$$\frac{60W}{9} = \frac{60}{9} = P_{total} = \frac{60}{9} \times 3 = 20W$$

A (100 W, 200V) bulb is connected to a 160 Volt supply. The power consumption would be

(a) 100 W

(b) 125 W

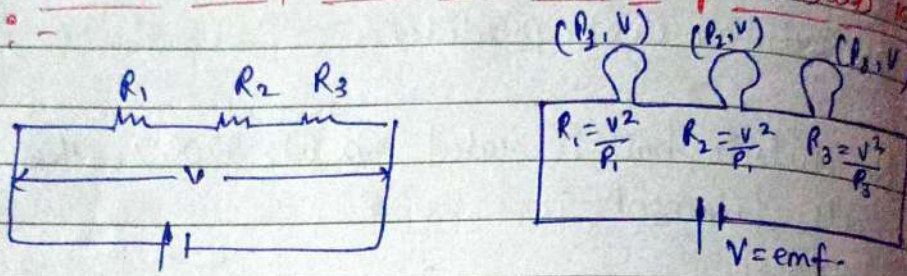
(c) 64 W

(d) 80 W

$$P_c = \left(\frac{V_s}{V_p}\right)^2 P_r = \left(\frac{160}{200}\right)^2 \times 100 \text{ W}$$

$$\frac{16}{25} \times 100 = 64 \text{ W } P_2$$

Series Combination of bulb (Power drop in Bulb in Series) :-



$$P_{\text{cons}} = \left[\frac{V^2}{R_{\text{eq}}} \right] = \frac{V^2}{R_1 + R_2 + R_3} = \frac{V^2}{\frac{V^2}{P_1} + \frac{V^2}{P_2} + \frac{V^2}{P_3}}$$

$$P_c = \frac{1}{\left(\frac{1}{P_1} + \frac{1}{P_2} + \frac{1}{P_3} \right)}$$

$$\boxed{\frac{1}{P_1} + \frac{1}{P_2} + \frac{1}{P_3} = \frac{1}{P_{\text{consum}}}}$$

Rated Power

Current is same in all bulb :-

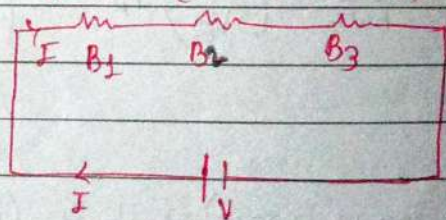
$$P_c = I^2 R_{\text{Bulb}}$$

$$P_{\text{con.}} \propto R_{\text{Bulb}} \propto \frac{1}{P_{\text{Rated}}}$$

$$\boxed{P_{\text{consumed}} \propto \frac{1}{P_{\text{Rated}}}}$$

$$R_1 = \frac{V^2}{60} \quad R_2 = \frac{V^2}{100} \quad R_3 = \frac{V^2}{200}$$

(60 W, V) (100 W, V) (200 W, V)

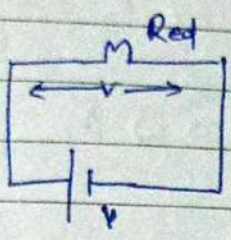


$$\boxed{B_3 > B_1 > B_2}$$

↑
Brightness of Bulb

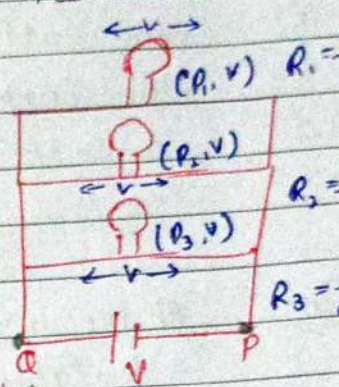
↳ Power consumed by Bulb

Parallel Combination of Bulbs (Power drop in Parallel Combination) :-



$$P_{total} = P_1 + P_2 + P_3$$

Compare their Brightness and Power consumed



$$P_{con} = \frac{V^2}{R_{bul}} = V^2 \left(\frac{1}{R_{eq}} \right)$$

$$\# P_{consumed} = \frac{V^2}{R_{bul}} \propto \frac{P_{rated}}{V_{rated}}$$

$$P_{con} = V^2 \left[\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right]$$

$$P_{consumed} \propto P_{rated}$$

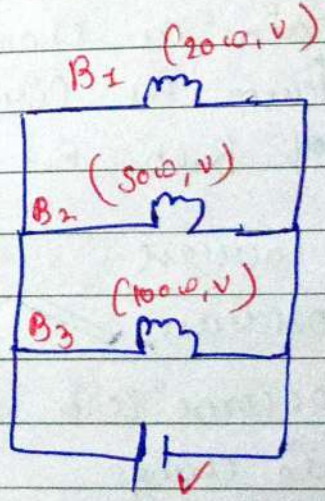
$$P_{con} = V^2 \left[\frac{P_1}{V^2} + \frac{P_2}{V^2} + \frac{P_3}{V^2} \right]$$

$$P_{con} = P_1 + P_2 + P_3$$

Compare their Brightness

$P_{con} \propto P_{rated}$

$$B_3 > B_2 > B_1$$



Two 220 Volt, 100 watt bulbs are connected first in series and then in parallel each time the combination is connected to a 220 Volt a.c supply line. The power drawn by the combination in each case respectively will be

- (a) 50 watt, 100 watt
- (b) 100 watt, 50 watt
- (c) 200 watt, 150 watt
- (d) 50 watt, 100 watt

$$\frac{1}{P} = \frac{1}{P_1} + \frac{1}{P_2}$$

$$\frac{1}{P} = \frac{1}{100} + \frac{1}{100} = P = 50 \text{ W}$$

$$P = P_1 + P_2 = 200 \text{ W}$$

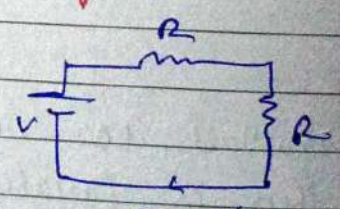
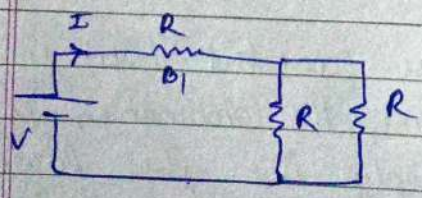
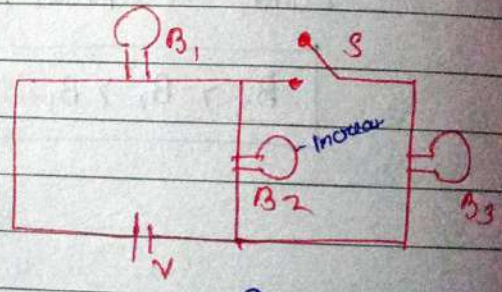
Ques. Of the two bulbs in a house held circuit one glows brighter than the other which of the two bulbs has a large resistance?

- (a) the bright bulb
- (b) the dim bulb
- (c) Both have the same resistance
- (d) the brightness does not depend upon the resistance

$$P_{\text{consum}} = \frac{V^2}{R_{\text{bulb}}}$$

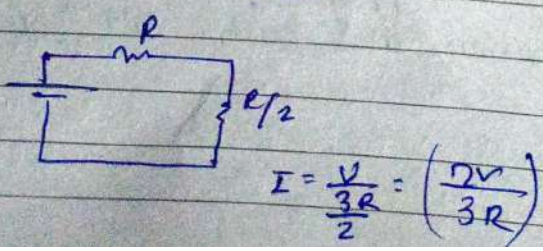
Ques. Three identical bulbs B_1, B_2, B_3 are connected to the main as shown in figure, if B_3 is disconnected from the circuit by opening switch S , then Incandescence of bulb B_1 will.

- (a) Increase
- (b) Decrease ✓
- (c) Become zero
- (d) No change



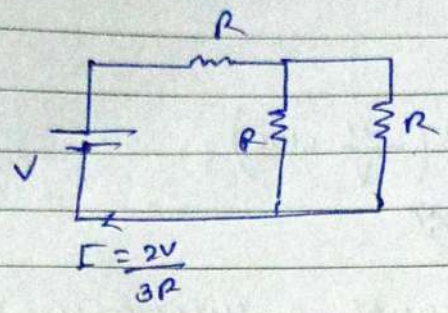
$$I = \frac{V}{2R}$$

$$P' = I^2 R = \frac{V^2}{4R^2} \cdot R = \frac{V^2}{4R}$$



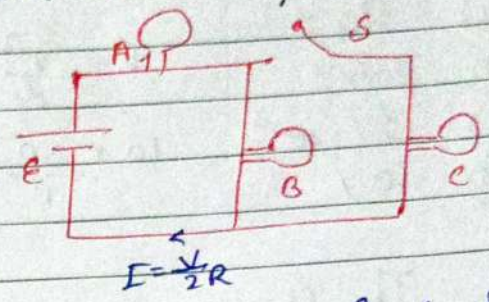
Three identical bulbs are connected as shown in figure when switch S is closed the power consumed in Bulb B is P. what will be the power consumed by the same bulb when switch S is opened.

- $\frac{9P}{4}$
- $\frac{16P}{9}$
- $\frac{9P}{16}$
- $\frac{4P}{9}$



$$P = I^2 R$$

$$\left(\frac{V}{3R}\right)^2 R = \frac{V^2}{9R} \oplus$$

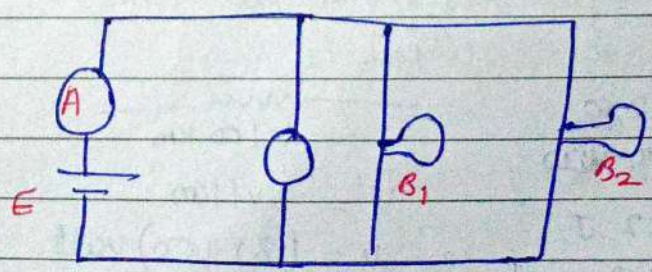


$$P' = I^2 R = \frac{V^2}{4R^2} R = \frac{V^2}{4R}$$

$P' = \frac{9P}{4}$

Two identical bulbs are connected in parallel across an ideal source of emf, E. The ammeter A and voltmeter V are ideal. If Bulb B₂ gets fused then

- Reading of A will increase but that of V will remain same.
- Reading of A will decrease but that of V will increase
- Reading of A will decrease but that of V will remain same.
- Reading of A will increase and reading of V will also increase.



Ques If Voltage across a bulb rated 220 Volt - 100 watt drops by 2.5% of its rated Value, the percentage of the rated Value by which the power would decrease is

- (a) 20%
 (b) 2.5%
 (c) 5% ✓
 (d) 10%

$$P = \frac{V^2}{R}$$

$$10 \times \frac{\Delta P}{P} = 2 \left(\frac{\Delta V}{V} \times 100 \right)$$

5%

Ques The charge flowing through a resistor R varies with time t as $Q = at - bt^2$ where a and b are positive constants. The total heat produced in R is

(a) $\frac{a^3 R}{2b}$

$$Q = at - bt^2$$

$$H = R \int (a - 2bt)^2 dt$$

(b) $\frac{a^3 R}{b}$

$$\frac{dQ}{dt} = I = a - 2bt$$

$$H = R \int (a - 2bt)^2 dt =$$

(c) $\frac{a^3 R}{6b}$

$$I = 0 = a - 2bt$$

$$R \left[\frac{(a - 2bt)^3}{3 \times (-2b)} \right]_0^{\frac{a}{2b}}$$

(d) $\frac{a^3 R}{3b}$

$$2bt = a$$

$$\boxed{t = \frac{a}{2b}}$$

$$\frac{R}{-6b} (0 - a^3)$$

$$dH = I^2 R dt$$

$$= \frac{a^3 R}{6b}$$

$$\int dH = \int (a - 2bt)^2 R dt$$

Ques Two cities are 150 km apart. Electric Power is sent from one city to another city through copper wires. The fall of potential per km is 8 Volt and the average resistance per km is 0.5Ω . The power loss in the wire is

- (a) 19.2 W
 (b) 19.2 kW ✓
 (c) 19.2 J
 (d) 12.2 kW

$$\frac{\text{---}}{d = 150 \text{ km}}$$

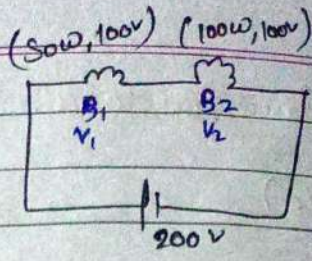
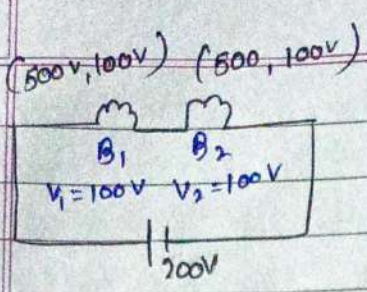
$$V' = 8 \text{ V/km}$$

$$V = (8 \times 150) \text{ Volt}$$

$$R = 0.5 \times 150 = 75 \Omega$$

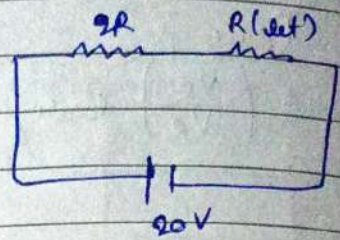
$$P = \frac{V^2}{R} = \frac{8 \times 8 \times 150 \times 150}{75}$$

$$64 \times 300$$



No Bulb will fuse

Total = $500 + 500$
100 watt



Page No: _____
Date: _____
Which Bulb will fuse?
 $x + 2x = 200$
 $3x = 200$
 $x = \frac{200}{3}$
 $V_1 = \frac{100}{3}$

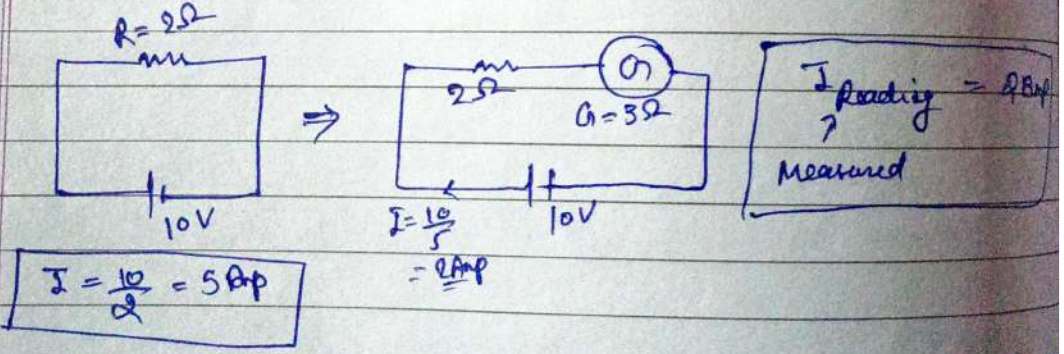
GALVANOMETER

- ⇒ Use to detect current, not to measure current.
- ⇒ Very sensitive, measure small current
- ⇒ Produce large error when connected in circuit

I_m = Maximum current can measure =
 G = Resistance of galvanometer

we have two problems
 ↗ High sensitivity
 ↘ Error.

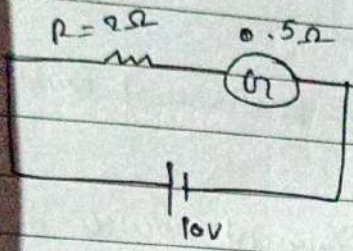
Galvanometer as Ammeter :- use to measure current



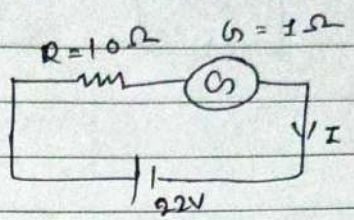
Find % error in the reading of galvanometer

$$\% \text{ error} = \frac{|I_m - I_T|}{I_T} \times 100$$

$$\frac{|2 - 5|}{5} \times 100 = 60\%$$



Ques



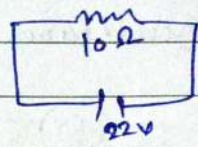
$$I_{\text{true}} = 5 \text{ Amp.}$$

$$I_m = \frac{10}{2.5} = 4 \text{ Amp.}$$

$$\% \text{ error} = \frac{|I_T - I_m|}{I_T} \times 100$$

$$= \frac{1}{5} \times 100 = 20\%$$

And % error in the reading of galvanometer.



$$I = \frac{22}{10} = 2.2 \text{ Amp}$$

$$\% \text{ error} = \frac{I_T - I_m}{I_T}$$

$$\frac{12.2 - 2}{2.2} \times 100$$

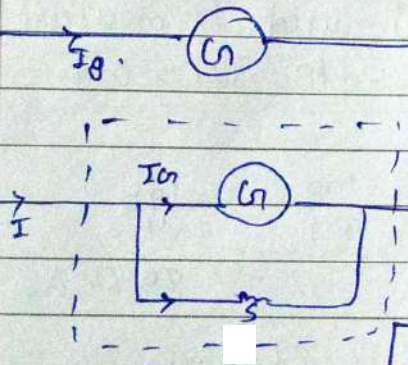
$$\frac{0.2}{2.2} \times 100$$

$$\frac{100}{11} = 9.09\%$$

Conversion of galvanometer into Ammeter.

Working Principle.

$$V_{\text{ammeter}} = V_G = V_{\text{shunt}}$$



$$R_a = \frac{GS}{G+S}$$

resist of ammeter.

Ideal ammeter

$$R_{\text{amm}} = 0 \leftarrow \text{Simple wire}$$

$$I_G G = (I - I_G) S$$

$$\text{If } I = n I_G \text{ --- (1)}$$

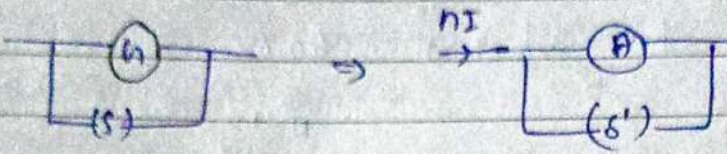
* Capacity of Ammeter increases by n times.

$$I_G G = (n I_G - I_G) S$$

$$G = (n-1) S$$

$$S = \frac{G}{n-1}$$

Conversion of Ammeter into Ammeter



$$S' = \frac{A}{n-1} \quad \text{Resistance of Ammeter}$$

Q10

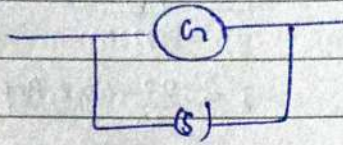
Ques In an ammeter 0.2% of main current passes through the galvanometer. If resistance of galvanometer is G . The resistance of ammeter will be

① $\frac{1}{499} G$

② $\frac{499}{800} G$

③ $\frac{1}{800} G$

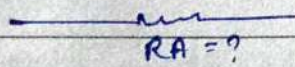
④ $\frac{500}{499} G$



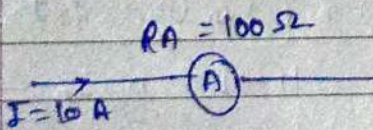
$$I_{RA} = 0.2\% I_n$$

$$R_A = \frac{0.2G}{100} = \frac{2G}{1000}$$

$$= \frac{G}{500} \Omega$$



Q11 Ammeter of resistance 100Ω is used to measure to A. Find resistance of shunt if we want to measure 50 A.



$$S = \frac{A}{n-1} = \frac{100}{5-1} = \frac{100}{4}$$

$$= 25 \Omega$$

Q12 A galvanometer of resistance G is shunted by a resistance S ohm. to keep the main current in the circuit unchanged. The resistance to be put in series with galvanometer is

① $\frac{G}{S+G}$

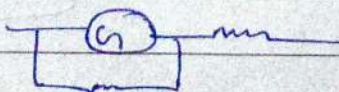
② $\frac{G}{S+G}$

③ $\frac{G^2}{S+G}$

④ $\frac{S^2}{S+G}$



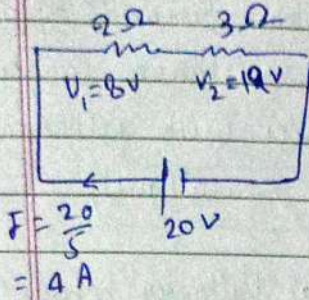
$$\frac{GS}{G+S} + R = G, \quad R = G - \frac{GS}{G+S}$$



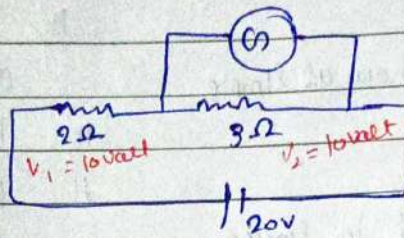
$$\frac{G^2 + GS - GS}{G+S}$$

$$R = \frac{G^2}{G+S}$$

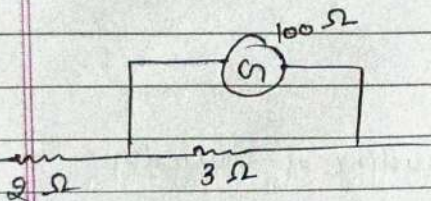
Galvanometer as a Voltmeter



If we want to measure potential drop across 3Ω , then we will use galvanometer parallel with 3Ω resistance.

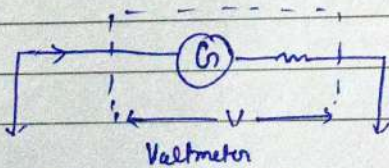
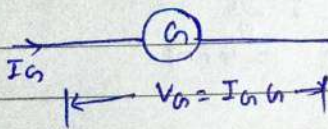


$$\% \text{ error} = \frac{V_T - V_m}{V_T} \times 100 = \frac{12 - 10}{12} \times 100 = \frac{100}{6} = 16\frac{2}{3}$$



$$\frac{100 \times 3}{103} = \frac{300}{103}$$

Conversion of galvanometer into Voltmeter



$$R_{\text{volt}} = G + S$$

Working Principle

$$V_G = I_G G \quad \text{--- (i)}$$

$$V_{\text{volt}} = I_G (G + S) \quad \text{--- (ii)}$$

$$\text{If } V_{\text{volt}} = n V_G \quad \text{--- (*)}$$

$$I_G (G + S) = n I_G G$$

$$G + S = nG$$

$$S = nG - G = G(n - 1)$$

Ammeter

- Ammeter formed by adding small resistance connected in parallel with galvanometer

$$S = \frac{G}{(n-1)}$$

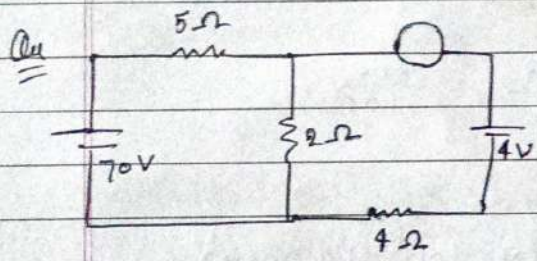
- # Ideal Ammeter behaves simple wire
- # $R_{ideal\ ammeter} = 0$
- # Ammeter connected in series in circuit where current have to measure

Voltmeter

- Voltmeter formed by adding large resistance connected in series with galvanometer

$$S = G(n-1)$$

- # Ideal Voltmeter behaves as open wire
- # $R_{ideal\ voltm} = \infty$
- # Voltmeter connected in parallel in circuit where potential have to measure

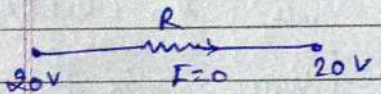
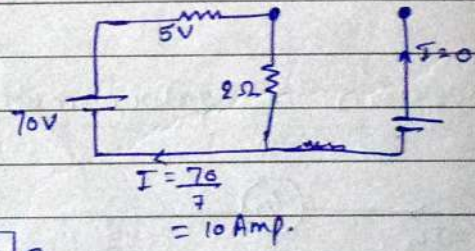


Find reading of Voltmeter = ?

$$V_A - IR + 4 = V_B$$

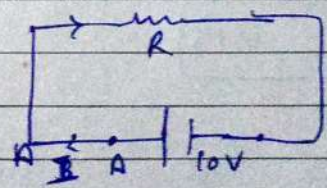
$$V_A - V_B = IR - 4$$

$$20 - 4 = \boxed{16\text{ Volt}} \text{ } \Omega$$



Current must be zero.

(20V) \rightarrow I may be (20V)
Zero or may not be zero.



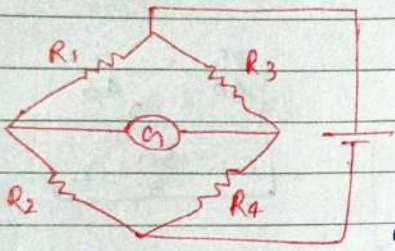
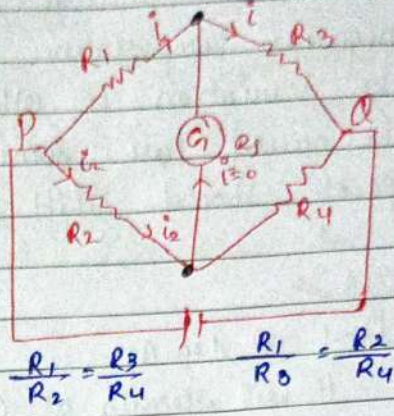
Wheatstone bridge

I_G will be zero, only when $V_A = V_B$

$$I.R \quad \frac{R_1}{R_2} = \frac{R_3}{R_4}$$

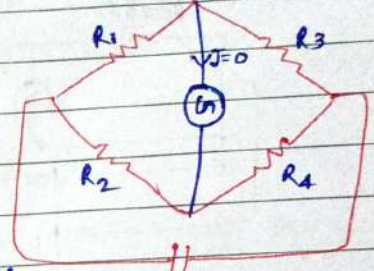
$$\frac{R_1}{R_3} = \frac{R_2}{R_4}$$

Balance Wheatstone Bridge



$$\frac{R_1}{R_2} = \frac{R_3}{R_4} = \text{same cond}^n.$$

Interchange the position of battery and galvanometer.



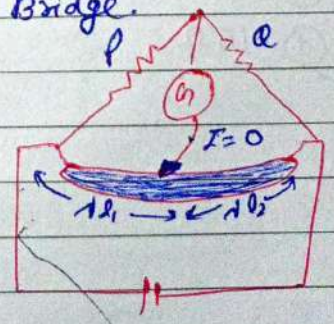
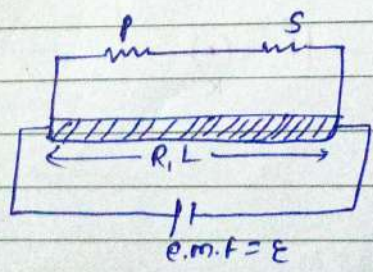
$$\frac{R_1}{R_2} = \frac{R_3}{R_4} \text{ --- Balance wheat Stone}$$

Meter Bridge

An instrument used to measure unknown resistance. Based on the concept of wheat stone bridge.

$$\frac{P}{l_1} = \frac{S}{l_2}$$

$$\frac{P}{S} = \frac{l_1}{l_2}$$



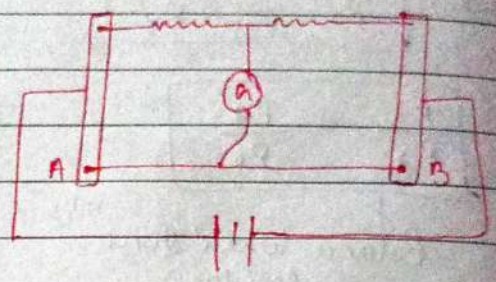
Resistance per unit length $\lambda = \frac{R}{L}$

If $L = 100 \text{ cm}$

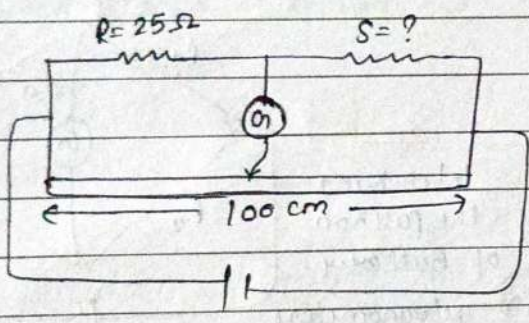
$$\text{then } \left(\frac{P}{S} = \frac{l_1}{100 - l_1} \right)$$

Ques In the meter bridge shown, the resistance X has a negative temperature coefficient of resistance. Neglecting the variation in other resistors, when current is passed for some time, in the circuit balance point should shift towards

- (a) A
- (b) B
- (c) First A then B
- (d) It will remain at C



Ques

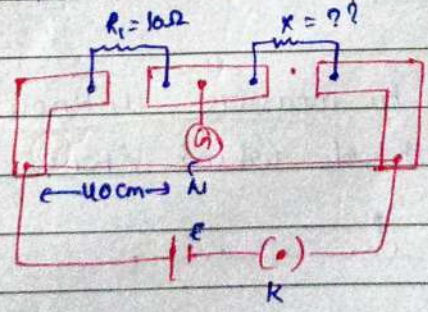


$$\frac{25}{3} = \frac{5}{2}$$

$$S = \frac{50}{2} \Omega$$

Ques In the meter bridge experiment, the null point is obtained at N. The value of unknown resistance X will

- (a) 60 ohms
- (b) 40 ohms
- (c) 6 ohms
- (d) 15 ohms



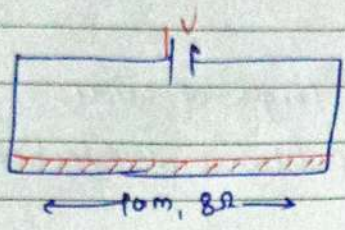
$$\frac{10}{40} = \frac{x}{60}$$

$$\frac{60}{4} = x$$

Unknown emf
with battery

Potentiometer wire

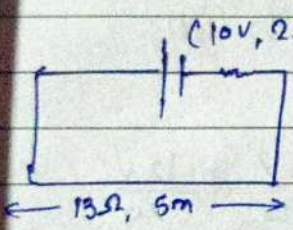
Potential drop in a metre - wire — Potential drop per unit length = $\frac{V}{L}$



Potential drop per unit length
 $= \frac{20}{10} = 2 \text{ V/m}$

$I = \frac{20}{8} \text{ Amp.}$

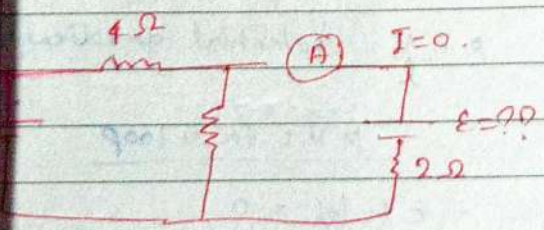
$V = IR = \frac{20}{8} \times 8 = 20 \text{ Volt}$



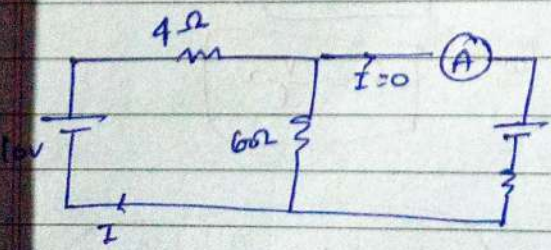
Potential drop per unit length = $\frac{V}{L} = \frac{26}{3 \times 5}$
 $= \frac{26}{15} \text{ V/m}$

$I = \frac{10}{15} = \frac{2}{3} \text{ Amp.}$

$V_{\text{wire}} = IR = \frac{2}{3} \times 13 = \frac{26}{3} \text{ Volt}$



If current in ammeter is zero then find E.M.F of unknown battery ??



KVL in loop

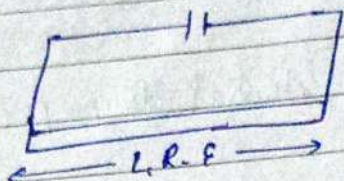
$0 + \epsilon - IR = 0$

$\epsilon = IR$

$1 \times 6 = 6 \text{ Volt}$

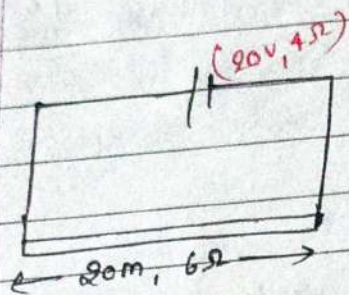
Based on potential gradient use to find

- e.m.f of cell
- Internal resistance
- ratio of e.m.f



L = length of wire
 R = Resistance of potentiometer wire

Que

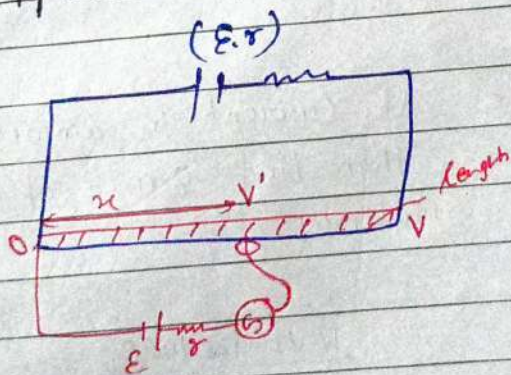


$$I = \frac{20}{10} = 2 \text{ Amp.}$$

$$V(\text{wire}) = IR = 2 \times 6 = 12 \text{ Volt}$$

$$\text{Potential drop per unit length} = \frac{V}{L} = \frac{12 \text{ V}}{20} = 0.6 \text{ V}$$

Application of Potentiometer wire - To find emf



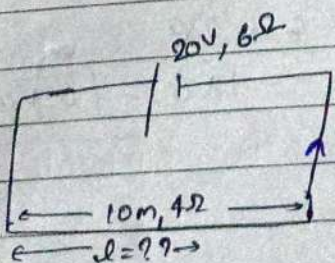
$$K = \frac{V}{l} = \text{Potential gradient}$$

K.V.L for a loop

$$-E + Kl = 0$$

$$E = Kl$$

$$\text{Formula } E = \frac{V}{l} x$$



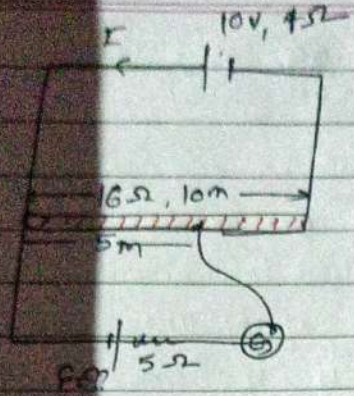
$$I = \frac{20}{10}$$

$$I = 2 \text{ A}$$

$$V = IR$$

$$V = 2 \times 4 = 8 \text{ Volt}$$

Ans Not Possible



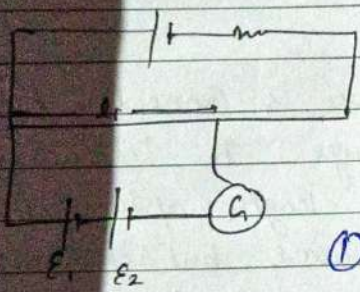
Find EMF of Battery = ?

Not possible
Balance point can't be find.

Application - 2

To compare emf of Battery

when both the battery is connected with some resistance then balance point is at l_1 .



(i) / (ii)

$$\frac{E_1 + E_2}{E_1 - E_2} = \frac{l}{l_2}$$

$$R l_1 = E_1 + E_2 \quad \text{--- (i)}$$

⇒ when polarity 2nd battery is reverse then balance condition is at l_2

$$R l_2 = E_1 - E_2 \quad \text{--- (ii)}$$

MR Path 4

$$\frac{E_1}{E_2} = \frac{l_1 + l_2}{l_1 - l_2}$$

Q. Two cells of emf E_1 and E_2 are to be compared in a potentiometer ($E_1 > E_2$) when the cells are used in series correctly. The balancing length obtained is 400 cm. when they are used in series but E_2 is connected with reverse polarity the balancing length obtained is 200 cm. Ratio of emf of cells is

- (a) 3:2 (b) 3:1 (c) 4:1 (d) 4:3

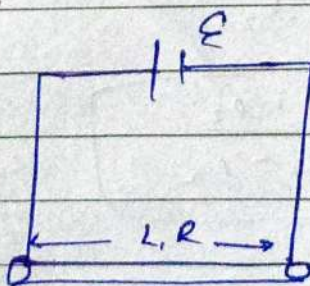
$$\frac{E_1}{E_2} = \frac{(400-200)}{(400-200)} = \frac{600}{200} = \frac{3}{1} \quad \text{A}$$

Ques Two cells of e.m.f E_1 and E_2 are joined in series and the balancing length of the potentiometer wire is 625 cm. If the terminal of E_1 are reversed the balancing length obtained is 125 cm. Given $E_2 > E_1$, the ratio $E_1 : E_2$ will be

- (1) 2:3 $\frac{E_2}{E_1} = \frac{l_1 + l_2}{l_1 + l_2}$
 (2) 3:1
 (3) 8:2 $\frac{E_2}{E_1} = \frac{750}{500} = \frac{3}{2}$
 (4) 1:5

Ques A 10 m long potentiometer wire is connected to a battery having a steady voltage. A Leclanche cell is balanced at 4 m length of the wire. If the length is kept the same, but its cross section is doubled, the null point will be obtained at.

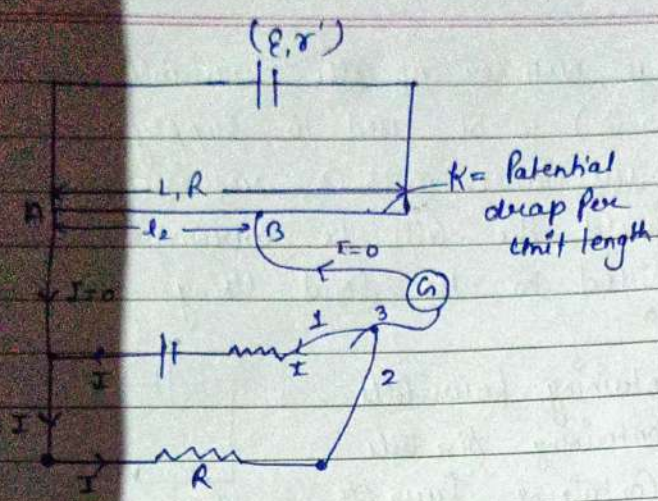
- (a) 8 m
 (b) 4 m
 (c) 2 m
 (d) None



$$k = \frac{E}{L}$$

Application - 3

To find internal resistance of cell



1st & 3rd key is connected.

Balance Point is at l_2 then $E = K l_2$ — (i)

Now 1st, 2nd & 3rd all are connected then point is at l_2 .

$$IR = K l_2 \text{ — (ii)}$$

$$\frac{ER}{R+r} = K l_2 \text{ — (iii)}$$

For Potentiometer

$$r = R \left(\frac{l_1}{l_2} - 1 \right)$$

For Rheostat

$$R = R \left(\frac{l_1}{l_2} - 1 \right)$$

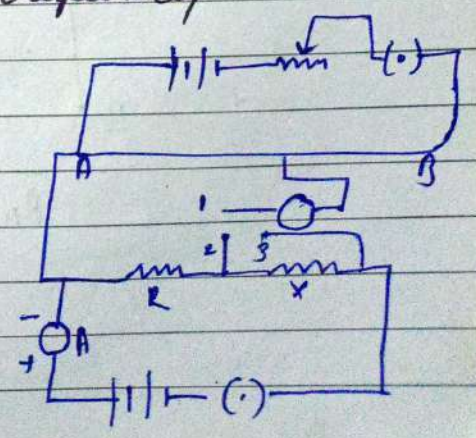
$$\frac{(i)}{(ii)}$$

$$\frac{E}{R+r} = \frac{K l_1}{K l_2} = \frac{R+r}{R} = \frac{l_1}{l_2}$$

$$\frac{R}{R} + \frac{r}{R} = \frac{l_1}{l_2} \Rightarrow \frac{r}{R} = \left(\frac{l_1}{l_2} - 1 \right)$$

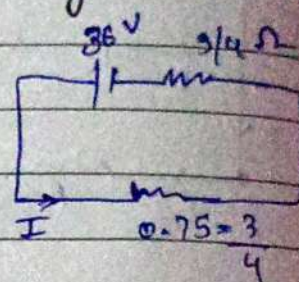
Ques A Potentiometer Circuit is set up as shown. The potential gradient across the potentiometer wire, is K Volt/cm and ammeter, present in the circuit, reads 1.0 A when two way key is switched off. The balance points when the key b/w the terminal (i) 1 and 2 (ii) 1 and 3 is plugged in, are found to be at length l_1 cm and l_2 cm respectively. The magnitude, of the resistor R and X , in ohms are then equal respectively to.

- (a) $K(l_2 - l_1)$ and $K l_1$
 - (b) $K(l_2 - l_1)$ and $K l_1$
 - (c) $K l_1$ and $K(l_2 - l_1)$
 - (d) $K(l_2 - l_1)$ and $K l_1$
- $$K l_1 = 1 \times R \text{ — (i)}$$
- $$K l_2 = 1(R + X) \text{ — (ii)}$$
- $$K l_2 = K l_1 + X$$
- $$K(l_2 - l_1) = X$$

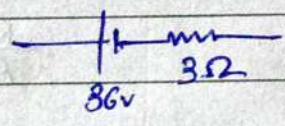
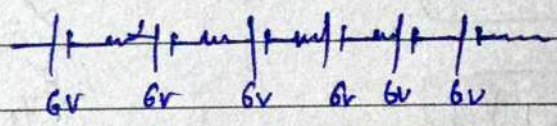
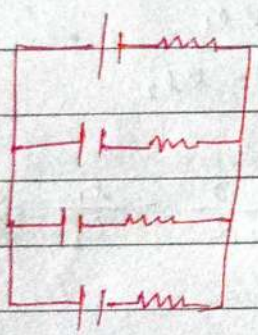


Ques There are a large number of cells available each marked (6V, 0.5Ω) to be used to supply current to a device of resistance 0.75Ω requiring 2A current. How should the cells be arranged so that power is transmitted to the load using minimum number of cells?

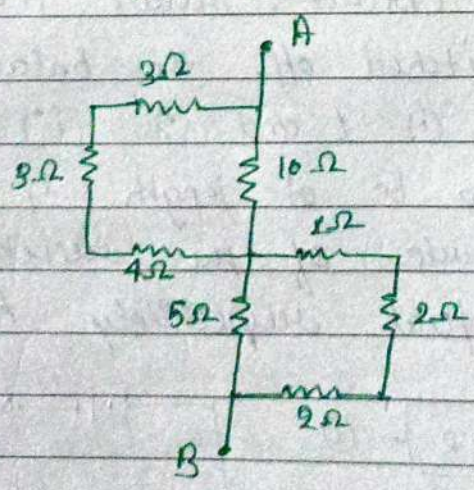
- (a) Six rows each containing four cells
- (b) four rows each containing six cells
- (c) four rows each containing four cells
- (d) Six rows each containing six cells



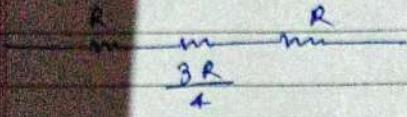
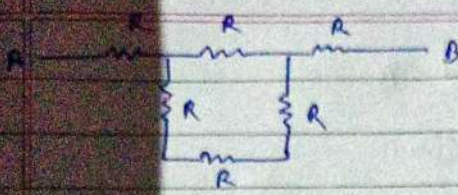
$$F = \frac{36}{\frac{3}{4} + \frac{3}{4}} = \frac{36 \times 4}{6} = 24$$



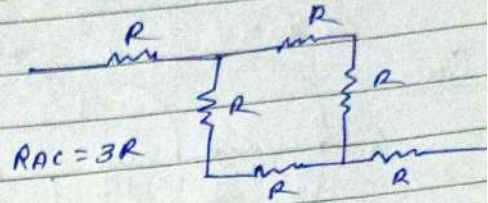
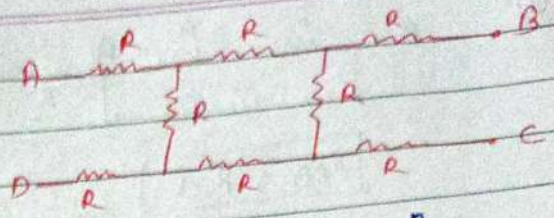
Finding of equivalent Resistance



$R_{AB} = 7.8 \Omega$



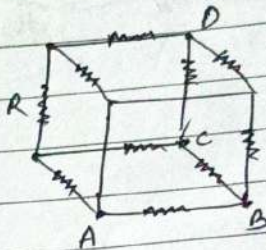
$$R_{AB} = 2R + \frac{3R}{4} = \frac{11R}{4}$$



$$R_{AC} = 3R$$

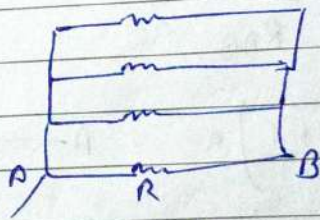
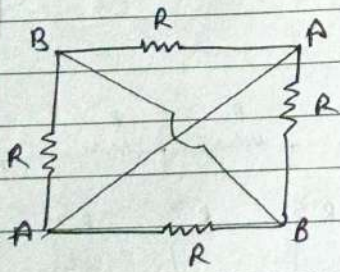
$$R_{AB} = \frac{7}{12} R \quad R_{AC} = \frac{3}{4} R$$

$$R_{AD} = \frac{5}{6} R$$

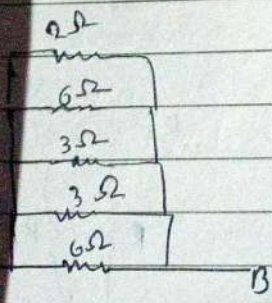


$$C_{AB} = \frac{12}{7} C \quad C_{AC} = \frac{4}{3} C \quad C_{AD} = \frac{6}{5} C$$

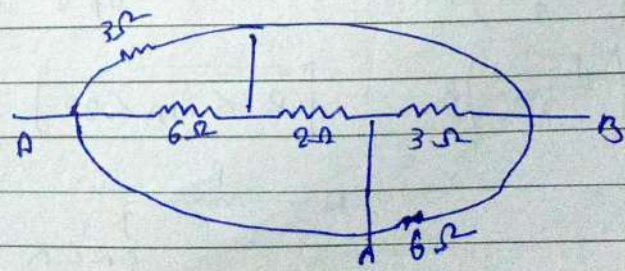
Find R_{AB} - (7)

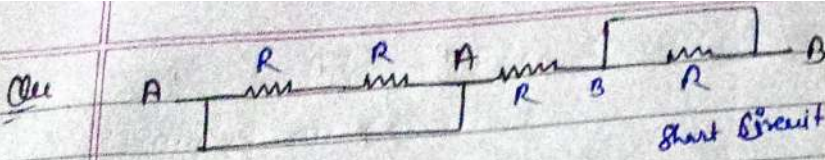


$$R_{AB} = \frac{R}{4}$$

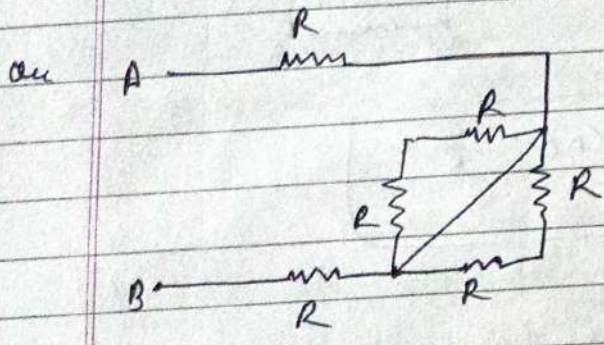
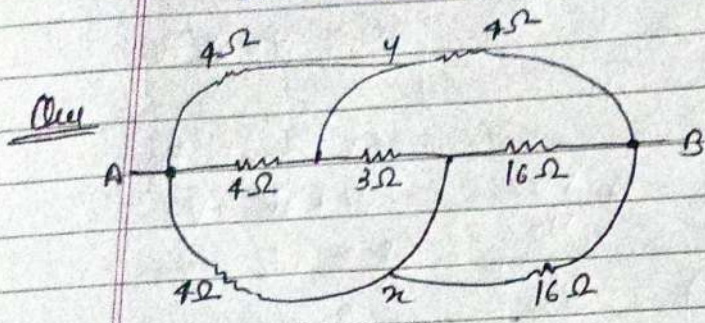


$$R_{AB} = \frac{2}{3} \Omega$$





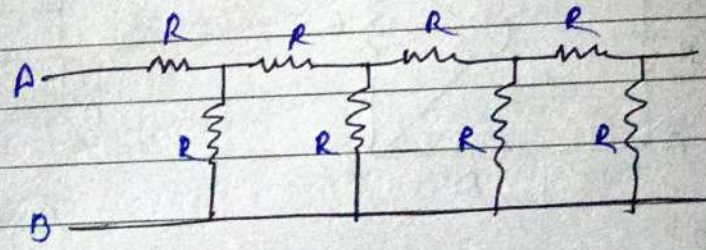
$R_{AB} = R/2$



$R_{AB} = 2R$

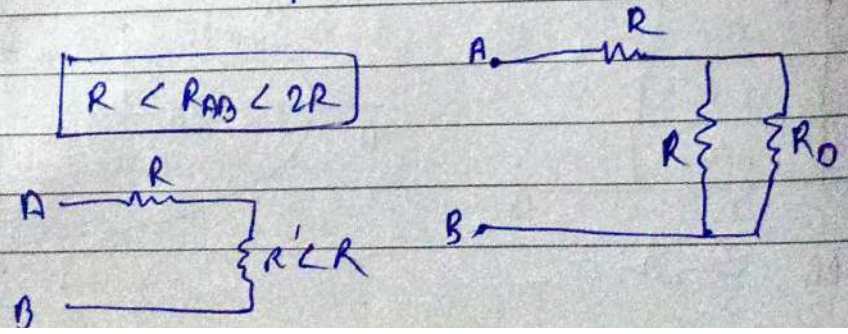
Ques Find $R_{AB} = ??$

- (a) $\left(\frac{\sqrt{5}+1}{2}\right)R$
- (b) $\left(\frac{\sqrt{5}-1}{2}\right)R$
- (c) $\left(\frac{\sqrt{3}+1}{4}\right)R$
- (d) $\left(\frac{\sqrt{3}-1}{2}\right)R$

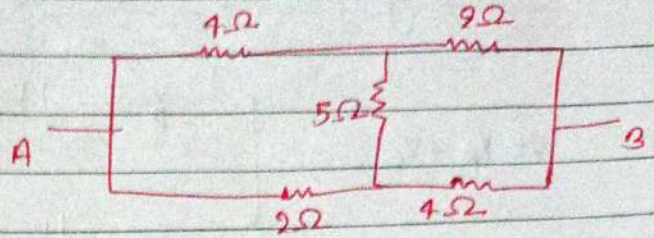
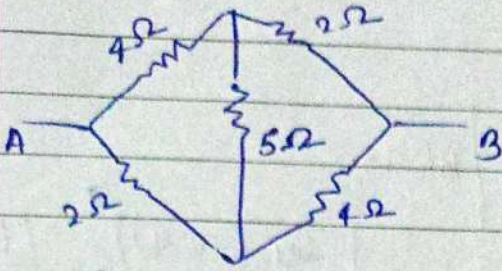


up to lmk

$R < R_{AB} < 2R$



UnBalance Wheatstone Bridge = Not in net



$$R_{AB} = 3\Omega$$

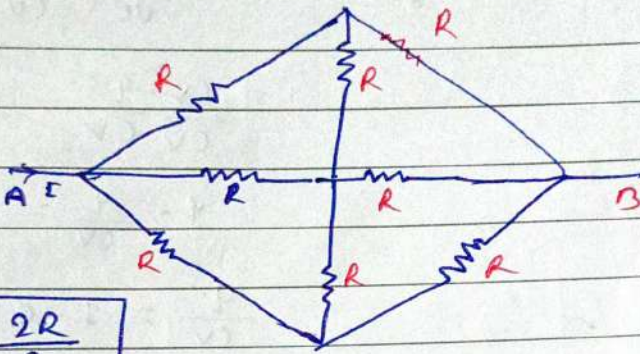
MR*

assume it is balance wheat stone bridge $R_{AB} = R_{AB} = 3\Omega$

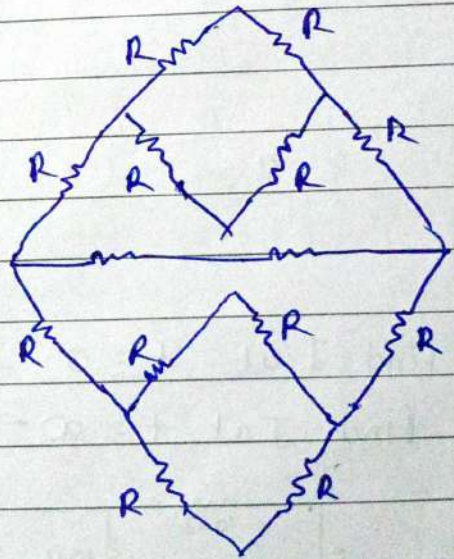
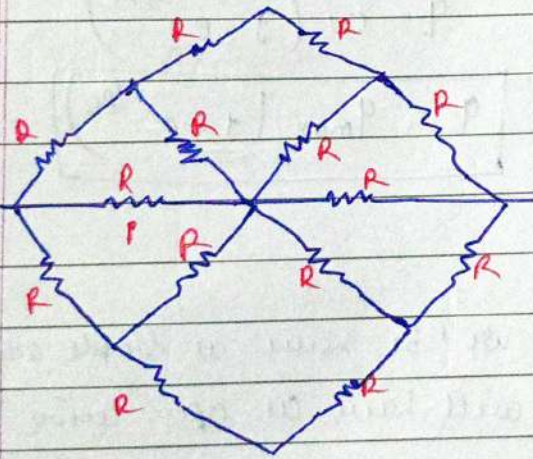
then find R_{AB} & your ans

will be just less than R_{AB}

$$= R = \frac{20}{7} \Omega$$



$$R_{AB} = \frac{2R}{3}$$



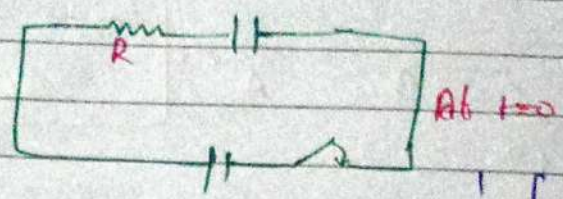
$$R_{AB} = \frac{\frac{3R \times 2R}{2} + 2R}{\frac{3R}{2} + 2R} = \frac{\frac{6R^2}{2}}{\frac{7R}{2}} = \frac{6R^2}{7R} = \frac{6}{7}R$$

$$\frac{6}{7}R$$

D/c \Rightarrow R/c Circuit

Charging an Capacitor

$V = V_R + V_c$



at time 't'

$V = V_R + V_c$

$V = IR + \frac{q}{c}$

$IR = V - \frac{q}{c}$

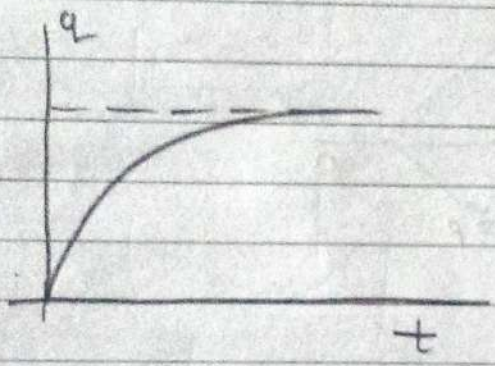
$\frac{dq}{dt} R = \frac{CV - q}{c}$

$\int_0^q \frac{dq}{CV - q} = \int_0^t \frac{dt}{RC}$

$\left[\frac{\log(CV - q)}{1} \right]_0^q = \frac{t}{RC}$

$\log(CV - q) - \log CV = -\frac{t}{RC}$

$\log \left(\frac{CV - q}{CV} \right) = -\frac{t}{RC}$



at steady state
 $t = \infty$

$q = q_{max} = CV$ depends on Resistance

$\frac{CV - q}{CV} = e^{-t/RC}$

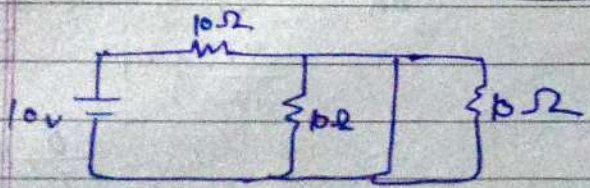
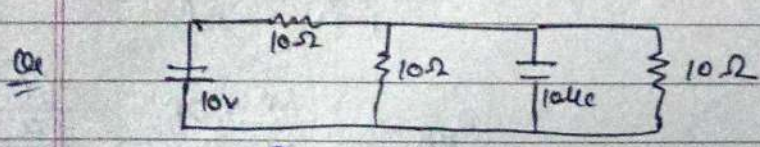
$1 - \frac{q}{CV} = e^{-t/RC}$

$\frac{q}{CV} = 1 - e^{-t/RC}$

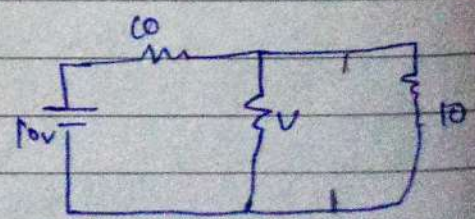
$q = CV (1 - e^{-t/RC})$

$q = q_{max} (1 - e^{-t/RC})$

- (i) find I at $t = 0 \rightarrow$ Capacitor will be have as simple wire
- (ii) find I at $t = \infty \rightarrow$ Capacitor will have as open wire



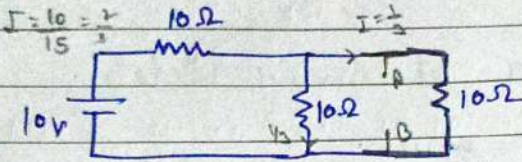
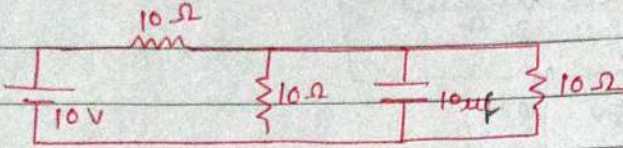
$I = \frac{10}{10} = 1 \text{ Amp}$



$I = \frac{10}{15} = \frac{2}{3} \text{ Amp}$

behaves open wire

Find charge on Capacitor in steady state

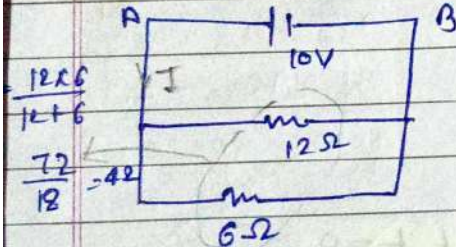
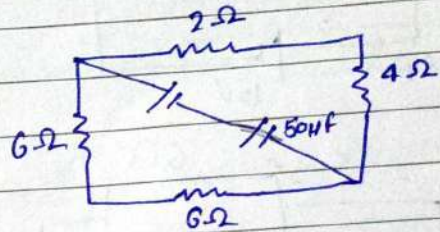


$$q = CV = 10 \times \frac{10}{3} = \frac{100}{3} \mu\text{C}$$

$$V_{AB} = \frac{10}{3} \text{ Volt}$$

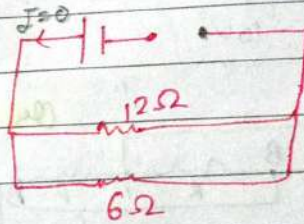
Find Current at $t=0$ and $t=\infty$ steady state.

Capacitor will behave as simple wire at $t=0$



$$I = \frac{V}{R} = \frac{10}{4} = 2.5 \text{ A}$$

at steady state \rightarrow Capacitor open wire

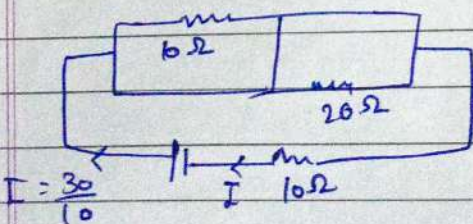


Charge on Capacitor $V_{cap} = 10 \text{ volt}$

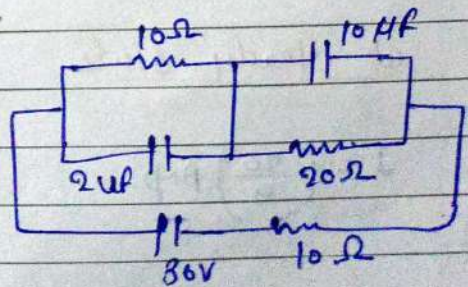
$$q = CV = 50 \times 10 = 500 \mu\text{C}$$

Find Current at $t=0$.

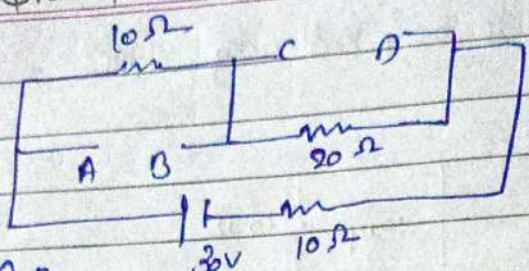
Capacitor \rightarrow simple wire



$$I = \frac{30}{10} = 3 \text{ A}$$

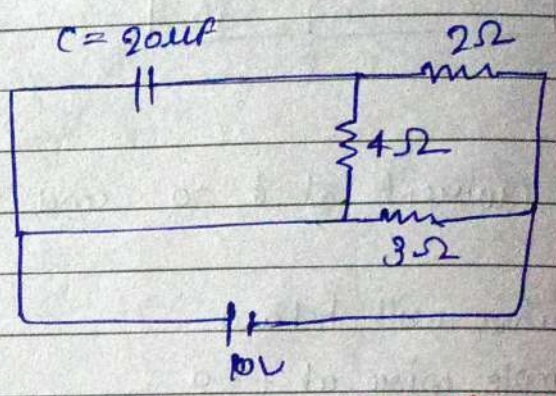
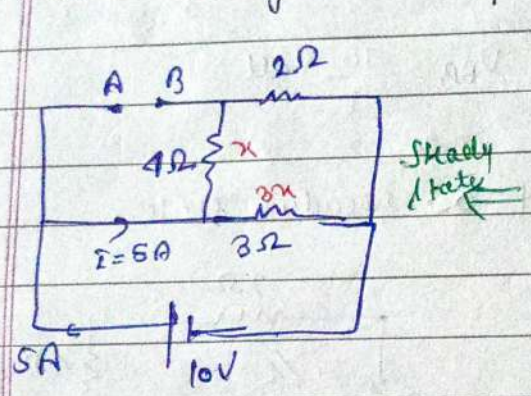


At Steady State.



$$I = \frac{30}{40} = \frac{3}{4} \text{ Amp}$$

find charge on Capacitor at Steady State.



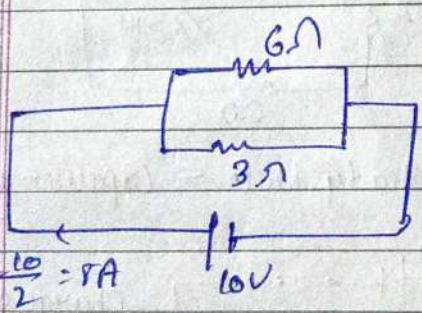
Steady State

Potential diff across capacitor

$$V_A - 4 \times \frac{5}{3} = V_B$$

$$V_A - V_C = V_C = \frac{20}{3}$$

$$q = CV = 20 \times \frac{20}{3} = \frac{400}{3}$$

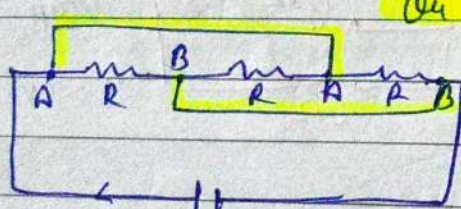


$$x = 2x = 5A$$

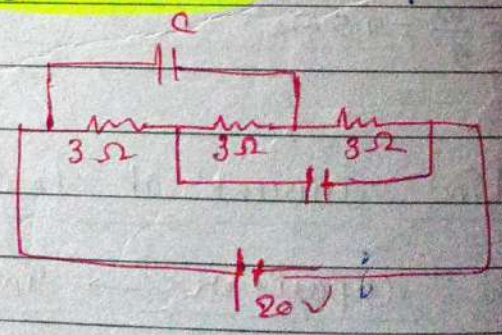
$$3x = 5A$$

$$x = \frac{5}{3} \text{ Amp}$$

Or find current $i = 0$



$$I = \frac{20}{9} = 2.22 \text{ Amp}$$

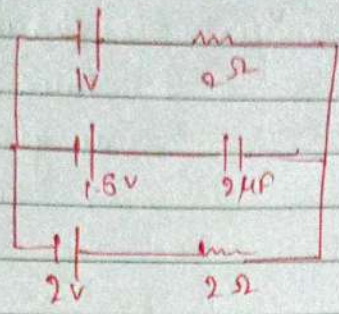


at Steady State

$$I = \left(\frac{20}{9} \right) \text{ Amp}$$

Q The charge in the 2 μF capacitor at steady state is

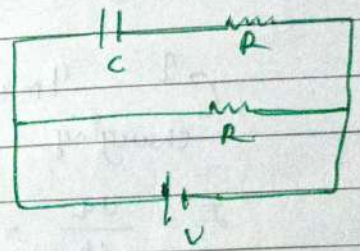
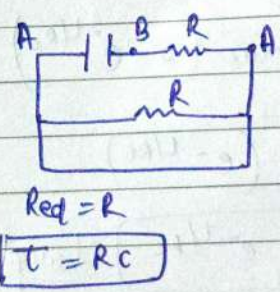
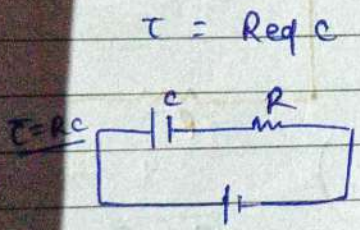
- ① zero
- ② 9 μC
- ③ 4 μC
- ④ 6 μC



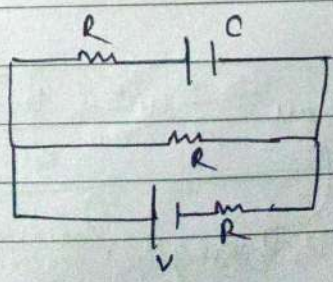
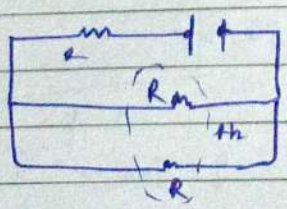
Time Constant $\tau = R_{eq} C$

Short circuit the battery and calculate **equivalent resistance** along **ends** of capacitor **$\tau = R_{eq} C$**

Find equivalent time const of circuit

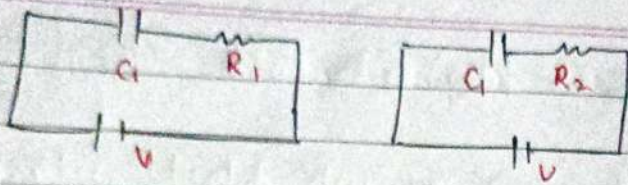


Q Find equivalent time constant

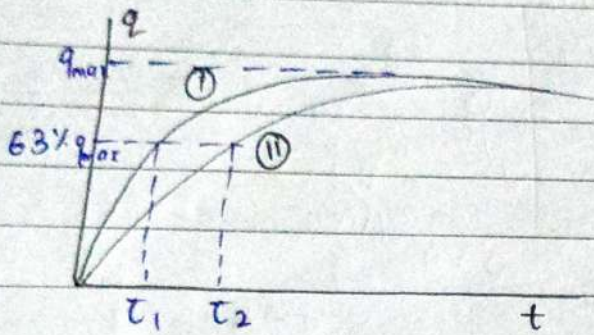


$$R_{AB} = R + \frac{R}{2} = \frac{3R}{2}$$

$$\tau = R_{eq} C = \frac{3RC}{2}$$



Compare C_1 & C_2 & R_1 & R_2



Charge q / time t
for both the curves
is give then compare
 C_2 and R_1 & R_2

q_{max} same on both capacitor

$$q_{max} = C_1 V = C_2 V$$

$$q_{max} = C_1 = C_2$$

$$\tau_1 < \tau_2$$

$$R_1 & C_1 < R_2 & C_2$$

$$R_1 < R_2$$

Discharging of Capacitor :-

$$q = q_{max} (1 - e^{-t/RC})$$

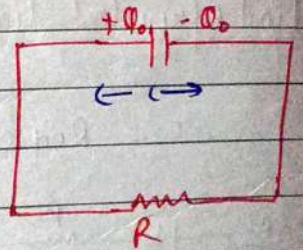
charging

$$I = \frac{dq}{dt} = q_{max} (0 - e^{-t/RC}) \left(-\frac{1}{RC}\right)$$

$$I = \frac{q_{max}}{RC} (e^{-t/RC})$$

$$I = I_{max} e^{-t/RC}$$

charging



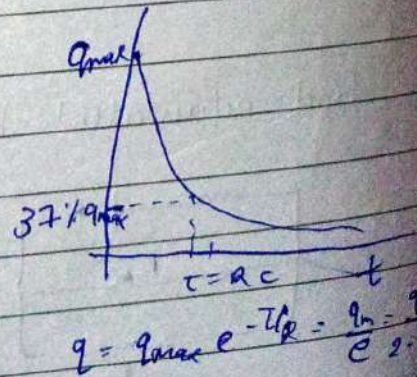
$$q = q_{max} e^{-t/RC}$$

$$q = q_{max} e^{-t/RC}$$

discharging

$$E_{max} = \frac{1}{2} C V^2 = \frac{q_{max}^2}{2C}$$

through Resistor



$$q = q_{max} e^{-t/RC} = \frac{q_{max}}{e^2}$$

Q4 Find Ratio of heat loss in R_1 and R_2

$$\frac{H_1}{H_2} \propto \frac{R_2}{R_1}$$

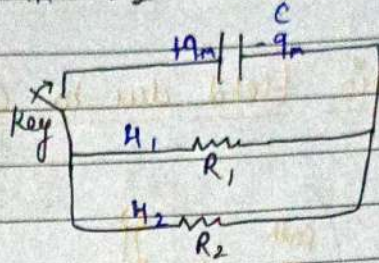
Ans

$$H = \frac{V^2}{R} t$$

Parallel
Combⁿ

$V = \text{Same}$

$$H \propto \frac{1}{R}$$



$$H_1 + H_2 = \frac{q_{max}^2}{2c}$$

$$H_1 + \frac{R_1 H_1}{R_2} = \frac{q_{max}^2}{2c}$$

$$H_1 \left(\frac{R_2 + R_1}{R_2} \right) = \frac{q_{max}^2}{2c}$$

$$H_1 = \frac{R_2}{R_1 + R_2} \left(\frac{q_{max}^2}{2c} \right)$$

$$H_2 = \frac{R_1}{R_1 + R_2} \left(\frac{q_{max}^2}{2c} \right)$$

Q4 Find Ratio of Heat loss through R_1 & R_2

$$H = I^2 R t$$

$$H \propto R$$

$$\frac{H_1}{H_2} = \frac{R_1}{R_2}$$

Ans

